

# Matrix Element Methods for Higgs phenomenology

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# Due to absence of signs of new physics

HEP has 'Big Mac' blues, i.e. why nature not like (as natural as) advertised?



# Commercial

Reality

Sure, it (Higgs boson) does the job, but...

## Improved/Unified way of interpretation of measurements

- interpretation of any measurement model dependent
- interpretation requires communication between different scales as well as theorists and experimentalists



#### Connecting measurements with UV physics

Kappa EFT Framework		Simplified Models	Full (UV) Model	
<ul> <li>NP models simple rescaling of couplings</li> </ul>	<ul> <li>SM degrees of freedom and symmetries</li> </ul>	<ul> <li>New low-energy degrees of freedom</li> </ul>	<ul> <li>Very complex and often high-dimensional parameter space</li> </ul>	
<ul> <li>No new Lorentz</li> <li>-structures or</li> <li>kinematics</li> </ul>	<ul> <li>New kinematics/ Lorentz structures</li> </ul>	<ul> <li>Subset of states of full models, reflective at scale of measurement</li> </ul>	<ul> <li>Allows to correlate high-scale and low- scale physics</li> </ul>	

#### Complexity/Flexibility

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## Coupling measurement during Run 1 using kappa-framework:





Higgs coupling fits based on total rates... no dynamics No new Lorentz structures, limited applicability for new physics

# Struggle for a unified language (basis) for Higgs EFT

#### Basis

- Complete
- Inspired by UV physics?

Several available:

Warsaw Basis SILH Basis Primary/Higgs Basis

[1008.4884] [hep-ph/070164] [1405.0181]

### Practicality

 Manageable number of operators for fit

# Validity

Validity range of EFT set by kinematic of measurement

#### Precision

- Resummation of large log (RGE improved pert. theory)
- ►Full NLO



### Basis and choice of operators to consider



#### Validity and Relevance of EFT



### Results for linearised LO EFT approach

Focus on linear contribution of EFT for theory prediction:

 $\mathcal{M} = \mathcal{M}_{\mathrm{SM}} + \mathcal{M}_{d=6}$ 

$$\mathcal{M}|^2 = |\mathcal{M}_{\rm SM}|^2 + 2\operatorname{Re}\{\mathcal{M}_{\rm SM}\mathcal{M}_{d=6}^*\} + \mathcal{O}(1/\Lambda^4)$$

<u>Number of predicted events:</u>  $N_{\rm th} = \sigma(H + X) \times BR(H \to YY)$ 

 $\times \mathcal{L} \times \mathrm{BR}(X, Y \to \mathrm{final \ state})$ 

[Englert, Kogler, Schulz, MS 1511.05170]

We assume that production and decay factorise to good approximation

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Each channel has own prod. and decay efficiencies:  $N_{\rm ev} = \epsilon_p \epsilon_d N_{\rm th}$ 

Wilson coefficients can be (over) constraint in many decay and production

processes: <u>Decays:</u>  $H \to f\bar{f}$   $H \to \gamma\gamma$   $H \to \gamma Z$  $H \to ZZ^* \quad H \to WW^*$ **<u>Production:</u>**  $pp \rightarrow H$   $pp \rightarrow Hj$   $pp \rightarrow Hjj$ 

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 $pp \to HV \quad pp \to ttH$ 

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signal strength:

36 indep. meas. (300 ifb) 46 indep. meas. (3000 ifb) differential:

88 indep. meas. (300 ifb) 123 indep. meas. (3000 ifb)

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#### signal strength measurement

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#### -0.05 -0.05 1.05 40 -30 -20 16 20 20 43 -16 and the second the second second -30 -20 -10 0 - 61 0 30 40 0 ς. 1.1.1.1.1.1 1 + 1 + 1standing for the strands of a adar 🖓 ar the second 40.00.00.00.00 10 20 20 40 50 -BH-GE-D4-BY B BY 0.4 0.0 C. 80 11 -39 -22 -19 0 13 Û, 0 20 30 -16 16 20 30 43 green = 300 ifb orange = 3000 ifb

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differential measurement



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#### Interpretation of results

Composite (SILH) Higgs:

One expects  $ar{c}_g \sim rac{m_W^2}{16\pi^2} rac{y_t^2}{\Lambda^2}$  with comp. scale  $\Lambda \sim g_
ho f$ with  $|\bar{c}_q| \lesssim 5 imes 10^{-6}$  we get  $\Lambda \gtrsim 2.8$  TeV

indirect probe of new physics scenario using Higgs observables only



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Global Fit allows to address most fundamental question for highenergy physics:

- Which theory calculations most important?
- Which systematic uncertainties most limiting?
- Where can we improve knowledge most?



Additional weakly-coupled light degree of freedom:

Affects only decay  $\Gamma_h = \Gamma_h^{
m SM} + \Gamma_h^{
m D6} + \Gamma_h^{
m inv}$ 

#### signal strength measurement



#### differential measurement



# Observations:

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- I. Methods chosen to communicate important (eff. theory, simp. model, ...)
  - The information extracted depends on the `picture', i.e. hypothesis, we compare with nature
  - The more precise the picture is we have in mind, the more precise will be the answer on the question of interest



- II. Higgs pheno and new physics searches request/benefit from high energies
  - EFT measurements
  - direct searches for new physics







Matrixelement method for jet- and met-rich final states

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- In Matrix Element our physics lacksquareunderstanding encoded
- MEM can improve S/B and S/sqrt(B)





- The more precise our physics picture, the better the discrimination
- MEM can improve S/B and S/sqrt(B)
- MEM provides direct connection between Lagrangian and Data
- Matrix Element Method does not need MC samples as opposed to BDT, NN, ...





# "The strange death of theory"



Frankfurter Allgemeine Zeitung 23.01.2017

# or is it?

Matrix Element Method vs Multi-variate Analysis (= pQCD = QFT)

- MVA well motivated to extract correlations without existing theory,
   i.e. stock trading or PDF fitting ;-)
- In particle physics we established gauge theories, thus, we have existing theory to predict connection of 'input with output'
- Current pheno approach:

We take first-principle QFT:  $\mathcal{L} = \mathcal{L}_{\mathrm{EW}} + \mathcal{L}_{\mathrm{QCD}} + \mathcal{L}_{\mathrm{Higgs}}$ 

Put it into an event generator to generate pseudo-data

Then a smart physicist or MVA comes up with way to access the Lagrangian we put in in the first place

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→ Seems like an unnecessary detour...

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# Training MVAs on Monte Carlo

 MVAs will optimise for – according to MC – most sensitive exclusive phase space regions

theory uncertainties difficult to control

- Full event generators are mashup of different parts that are partly tuned, i.e. hard interaction, UE, ISR, hadronisation, ...
- Highly computationally intensive. If you want to template correlations of say 7 particles:
  - Time estimate:

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7 microjets, each 4-momentum components divided into only 10 bins -> 10<sup>28</sup>/7! ~ 10<sup>24</sup> configurations If MC takes 1 ms per event -> 10<sup>13</sup> years to have 1 hit per config.

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# Training MVAs on data only

- Less plagued by systematics
- But only possible if objects to reconstruct or events to measure already in data.
   -> oxymoron for discovery of anything new,
   e.g. gluino-tag, axion-tag, pp->HH->4b,...
- Everything done purely on data without theory cross-check has 0 safety margins...

⇒2 TeV excess in ATLAS and CMS might be an example (though I am not saying that anything was done wrongly) see [Goncalves, Krauss, MS '15]









Ideally one would like to use all radiation related to hard process to discriminate signal from background



# Applications of Matrix Element Method:

1988	Rec. of events with MET		[Kondo, J.Phys.Soc.Jap. (1988)]		
1998	Anomalous gauge	couplings	[Diehl, Nachtmann Eur. Phys. J. C1 (1998)]		
2005	top quark physics	[Abazov et	al., Nature (2004), DO Collab.]		
		[Abulencia et al., PRD 73 (2005), CDF Collab.]			
		[Abazov et	al., PLB 617 (2005), DO Collab.]		

2010 Automated implementation in MadWeight [Artoisenet et al, JHEP 1012 (2010)]

# Plenty of recent applications in Higgs physics:

- $\begin{array}{ll} H \rightarrow \mu^{+}\mu^{-} & [ \texttt{Cranmer, Plehn EPJC 51 (2007)} \\ H \rightarrow b\bar{b} & [ \texttt{Soper, MS PRD 84 (2011)} \\ H \rightarrow \gamma\gamma & [ \texttt{Andersen, Englert, MS PRD 84 (2013)} \\ pp \rightarrow t\bar{t}H & [ \texttt{Artoisenet et al. PRL 111 (2013)} ] \end{array}$
- $H \rightarrow ZZ^*/WW^*/Z\gamma$  [Campbell et al JHEP 1211 (2012)] [Freitas et al PRD 88 (2013)] [Campbell et al PRD 87 (2013)]

Spin/Parity [Avery, et al. PRD 87 (2013)] [Gao et al. PRD 81 (2010)]

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#### The matrix element method in a nutshell:

Given a theoretical assumption  $\alpha$ , attach a weight  $P(\mathbf{x}, \alpha)$  to each experimental event **x** quantifying the validity of the theoretical assumption for this event.

$$P(\mathbf{x}, \alpha) = \frac{1}{\sigma} \int d\phi(\mathbf{y}) |M_{\alpha}|^{2}(\mathbf{y}) W(\mathbf{x}, \mathbf{y})$$

- $|M_{\alpha}|^2$  is squared matrix element
- $W(\mathbf{x}, \mathbf{y})$  is the resolution or transfer function
  - $d\phi(\mathbf{y})$  is the parton-level phase-space measure

The value of the weight  $P(\mathbf{x}, \alpha)$  is the probability to observe the experimental event **x** in the theoretical frame  $\alpha$ 

Purpose of the transfer function is to match jets to partons



Probability density function: 
$$\int d\mathbf{y} \ W(\mathbf{x}, \mathbf{y}) = 1$$

#### The form of the transfer function:

resolution in







azimuthal angle



Complex, high-dimensional gaussian distribution! Transfer function introduces new peaks on top of propagators

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Subtleties of the convolution  $|M(y)|^2 \times W(y,x)$ 

- 1)  $|M(y)|^2$ 
  - Can be calculated at different order in pert. series (LO, NLO)
  - Final state multiplicity fixed (exclusive process)
  - Some kinematic configurations induce large logs (need resummation)

2) W(y, x)

- Number of final state objects limited to exclusive process
- Integration very time consuming -> limits final state multiplicity

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• Transfer function fit dependent (input from experiment)

Two objects that prove to be challenging for MEM (mapping to matrix element)

- Jet-rich final state
  - jet -> parton mapping difficult, i.e. depends on jet definition, detector response
  - many sources of jets at hadron colliders, i.e. particle multiplicity of hard process, not jet multiplicity of event
- MET-rich final state
  - ➡ MET -> particle mapping difficult, i.e. only indirect information about particle

# We want to study more objects in final state -> Transfer function limits us. Do we always need it? Transfer functions only important if matrix element varies quickly:



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We want to study more objects in final state -> Transfer function limits us. Do we always need it? Transfer functions only important if matrix element varies quickly:



Higgs reconstructed, but no transfer function for jets:



# After removing transfer function we can improve on precision of matrix element $|M(y)|^2$

Matrix element method at NLO:

[Campbell, Giele, Williams JHEP 1211 (2012)] [Martini, Uwer '15 '17] [Gritsanen et al '16]

boost

Boost along transverse and longitudinal direction such that LO final state multiplicity momenta balance

> Born phase space, but long. boost not unique, need longitud. integration

Calculate virtual for born topology real for jet function

$$\mathcal{P}_{NLO}^{MEM}(\{Q_n\}) = rac{1}{\sigma_{NLO}} \int_{x_{min}}^{x_{max}} dx_1 \mathcal{P}_{NLO}(\Phi_B)$$

$$\eta^{lab,i} = \frac{1}{2} \log \left( \frac{x_a^2 s}{s_{ab}} \frac{s_{ib}}{s_{ai}} \right)$$



Application to H->4l (boost easier to identify)

sensitivity LO vs NLO improvement ~ 10%

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# Remove limitation of final state objects on $|M(y)|^2$

Factorization of emissions in soft/collinear limit [Soper, MS PRD 84 (2011)]

and Sudakov factors allow semiclassical approximation of quantum process:



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# Can improve reconstruction for tops and Higgs

make use of many properties of the top for reconstruction (top mass, W mass, EW structure of decay)

However, QCD radiation pattern are left mostly aside.





Radiation off bottom quark down to

angular distribution for radiation

# One can be more quantitative...

use emission prob. from [Soper, MS PRD 87]



pT top 500 GeV, pT gluon 20 GeV



Wrapping up all factors gives weight for shower history

$$\chi = \frac{\sum_{ISR/Hard} \left( \sum_{i} \text{ISR}_{i} \times \sum_{j} \text{Signal}_{j} \right)}{\sum_{ISR/Hard} \left( \sum_{i} \text{ISR}_{i} \times \sum_{j} \text{Backg}_{j} \right)}$$

Here  $Signal_1 = H_H H_{split} e^{-S_{split}} H_{bbg} e^{-S'_b} e^{-S''_b} e^{-S'_g} H'_{bbg} e^{-S'_b} e^{-S'_g}$ 

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And many more...

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And for all backgrounds...

Analogously for the top decay (more involved as top colored)



Conceptional difference compared to Higgs from last year:

- Splitting functions for massive emitter and spectator
- Full matrix element for top decay

$$\chi(\{p,t\}_N) = \frac{P(\{p,t\}_N|\mathbf{S})}{P(\{p,t\}_N|\mathbf{B})} = \frac{\sum_{\text{histories}} H_{ISR} \cdots \sum_{\text{histories}} |\mathcal{M}|^2 H_{\text{top}} e^{-S_{t_1}} H_{tg}^s e^{-S_g} \cdots}{\sum_{\text{histories}} H_{ISR} \cdots \sum_{\text{histories}} H_g^b e^{S_g} H_{ggg} \cdots}$$

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# Results by CMS



code available at https://www.ippp.dur.ac.uk/~mspannow/shower-deconstruction.html

# First application of Event Deconstruction

[Soper, MS '14]

fully hadronic  $Z' \rightarrow tt$ 



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#### Measuring the Higgs-bottom coupling in VBF



Attempt of cut and count analysis [Mangano, et al '02]

$m_H$	$115~{\rm GeV}$	$120 { m GeV}$	$140 { m GeV}$	
Signal	$1.3 \times 10^3$	$1.2 \times 10^3$	$5.2 \times 10^2$	
$b\bar{b}jj$	$2.4 \times 10^5$	$2.3 \times 10^5$	$1.9 \times 10^5$	
j <sub>b</sub> j <sub>b</sub> jj	$2.6 \times 10^3$	$2.3 \times 10^3$	$1.8 \times 10^3$	and a state of the second
$(Z^*/\gamma^* \to b\bar{b})jj$	$1.1 \times 10^2$	$6.6 \times 10^1$	$1.3 \times 10^1$	
$(Z \to b\bar{b})_{\rm res} jj$	$6.2 \times 10^2$	$3.4 \times 10^2$	$0.5 \times 10^1$	
$j_b j \oplus j_b j$	$2.9 \times 10^2$	$3.2 \times 10^2$	$4.5 \times 10^2$	

Table 3: Same as Table 1, with  $p_{\rm T}^j > 80$  GeV.

S/B ~ 1/200 Will render channel due to systematic uncertainties insensitive





However, matrix element and shower still discriminative

![](_page_51_Figure_4.jpeg)

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[Englert, Mattelaer, MS `15]

		WBF	GF	bājj	$Z_{jj}$	3333
(i)	fat jet	48.50	17.32	205109	553.16	$2.23 \cdot 10^{7}$
(ii)	wbf cuts	21.23	4.11	48441.9	127.98	$5.18\cdot 10^6$
(iii)	mercedes star	18.44	2.82	31674.5	84.975	$3.39 \cdot 10^6$
(iv)	fatjet b-tags	4.69	0.578	3800.99	12.57	323.74

#### Standard cuts are not discriminative enough

![](_page_51_Figure_8.jpeg)

 $0.82 < y_b/y_b^{\rm SM} < 1.14$  with 600 ifb

# tth: di-lepton vs semileptonic channel

![](_page_52_Figure_1.jpeg)

- Analysis with 4 b-jets and std ٠ reconstruction as input to MEM
- Full integration over invisible particles

#### 0.4 signal events (D<sub>S</sub>) bg. events (D<sub>B</sub>) 0.2di-lepton channel 0 0.2 single-lepton channel 0 0.6 0.8 0.20.4 0 D $D_i = \frac{P(x_i|S)}{P(x_i|S) + P(x_i|B)}$

Projection at 14 TeV

#### [Artoisenet et al. PRL 111 (2013)]

process	incl. $\sigma$	efficiency	$\sigma^{ m rec}$
$t\bar{t}h$ , single-lepton	111 fb	0.0485	$5.37 \ \mathrm{fb}$
$t\bar{t}h$ , di-lepton	$17.7 \ \mathrm{fb}$	0.0359	0.634 fb
$t\bar{t}$ +jets, single-lepton	256  pb	$0.463 \times 10^{-3}$	119 fb
$t\bar{t}$ +jets, di-lepton	40.9 pb	$0.168 \times 10^{-3}$	$6.89 \ \mathrm{fb}$

![](_page_53_Figure_8.jpeg)

- Using Matrix Element Method dilepton channel as or more sensitive than single-lepton channel
- However, single-lepton channel uses standard input, boosted region not captured [Plehn, Salam, MS PRL 104 (2009)]

# Maximisation vs Integration

 $\bullet$  To speed up the evaluation one can maximise over the phase space volume  $\Phi$  , rather than integrate

$$w_{\alpha}(x) = \max_{y \in \Phi} \left( |M_{\alpha}|^2(y)W(x,y) \right)$$

Generic method for multiple source of MEM

Example:  $pp \rightarrow H \rightarrow W^+W^-$  with  $W^+W^- \rightarrow \mu^+\nu_\mu\mu^-\bar{\nu}_\mu$ 

![](_page_54_Figure_5.jpeg)

![](_page_55_Figure_0.jpeg)

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Strong improvement in S/B on top of event selection and purification cuts on visible objects

![](_page_56_Figure_1.jpeg)

		10181101	Dackground	0/0	5/ 0
	Basic event selection cuts	327	11451	0.029	3.058
	Assuming perfec	et $E_T^{\text{miss}}$	reconstructi	on	
	Veto $\chi S, B(S, B) = 0$	299	3724	0.080	4.912
limit already	$\log(\chi) > 1$	262	2200	0.119	5.592
better than	$\log(\chi) > 1.5$	118	808	0.146	4.157
ATI AS combined	Assuming a 10%	resuluti	on effect in $E$	$T^{\rm miss}_T$	
AILAS combined	Veto $w_{S,B}(S,B) = 0$	294	3742	0.079	4.806
7 + 8 TeV data 🥖	$\ell$ $\log(\chi) > 1$	256	2204	0.116	5.455
	$\log(\chi) > 1.5$	114	811	0.141	4.016
	$g_{H,WW} \in [0.6]$	5, 1.25	$]  imes g_{H,WW,K}$	<i>sм</i> а1	+ 95% CL
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# Summary

- Matrix Element Method is active field of research
- Current interest in machine-learning is not taking matrix element methods out of the picture! MEM can help to check MVAs
- MEM can be discovery tool

• My personal view:

![](_page_57_Figure_5.jpeg)

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Cure from Big Mac Blues

# Summary

- Matrix Element Method is active field of research
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- MEM can be discovery tool
- My personal view:

![](_page_58_Figure_5.jpeg)

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• My personal view:

![](_page_59_Figure_6.jpeg)

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