

Finite Temperature Effects in Dark Matter Production

Joachim Kopp

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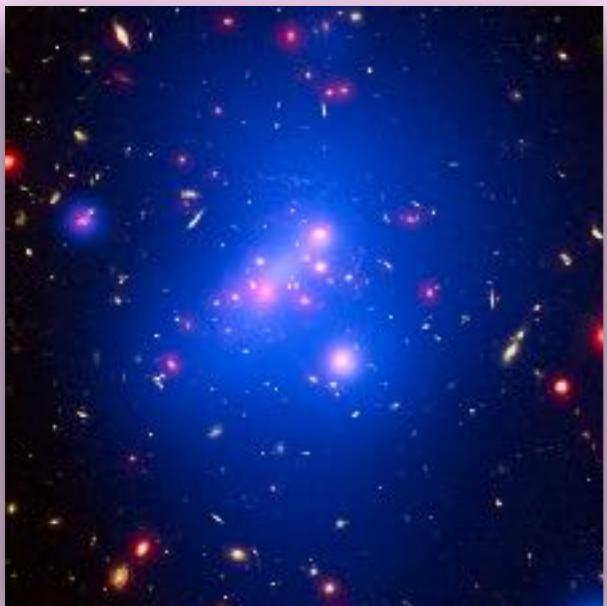


Evidence for Dark Matter

The Slide You've Seen 1000 Times

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Galaxy Clusters

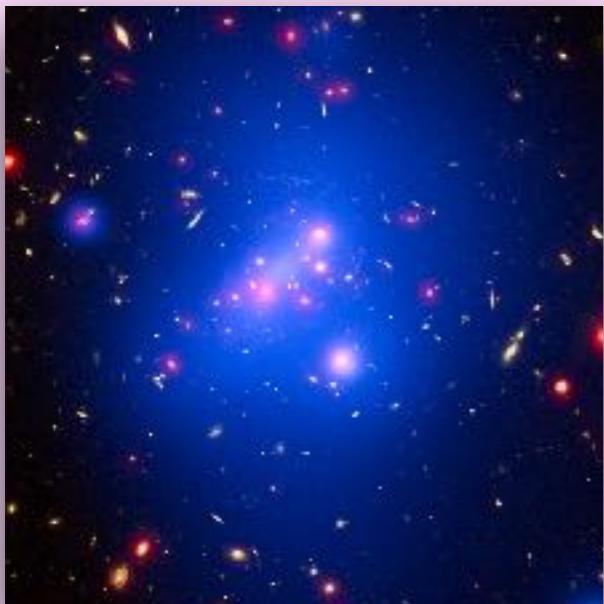


Virial Theorem: $E_{\text{kin}} = -\frac{1}{2}E_{\text{pot}}$

Zwicky, 1930s: $E_{\text{kin}} = -\frac{1}{2}E_{\text{pot}} \times 170$

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Galaxy Clusters

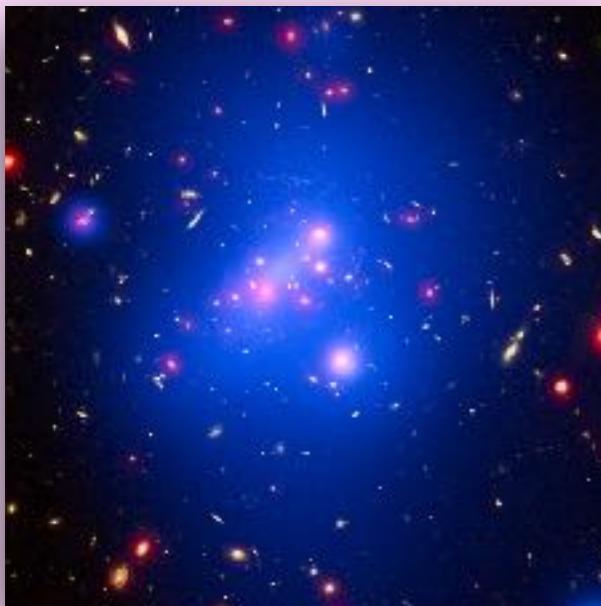


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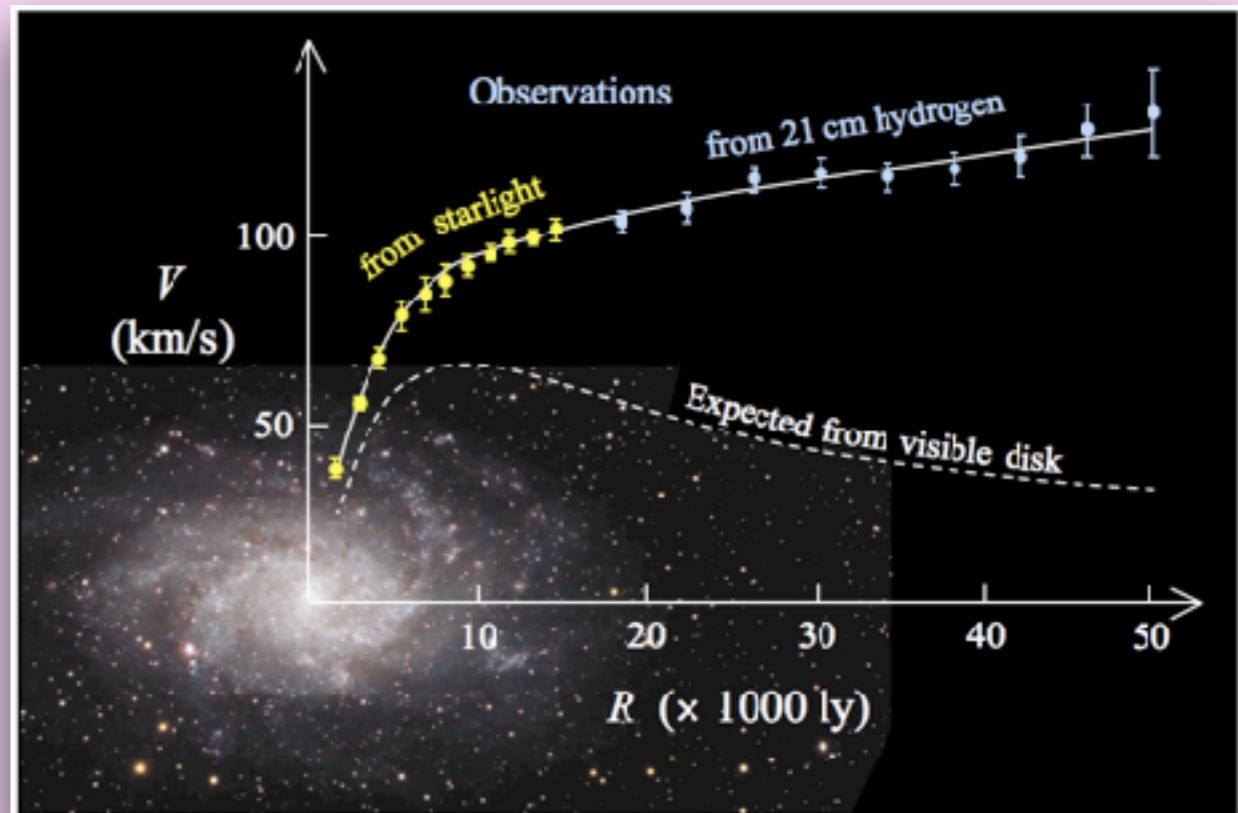
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Galaxy Clusters



Galaxy Rotation Curves



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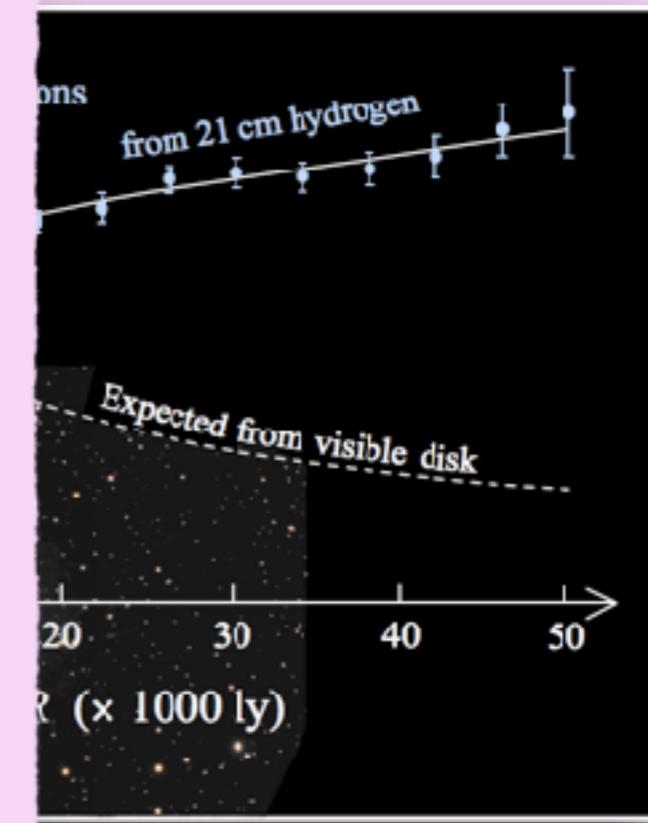
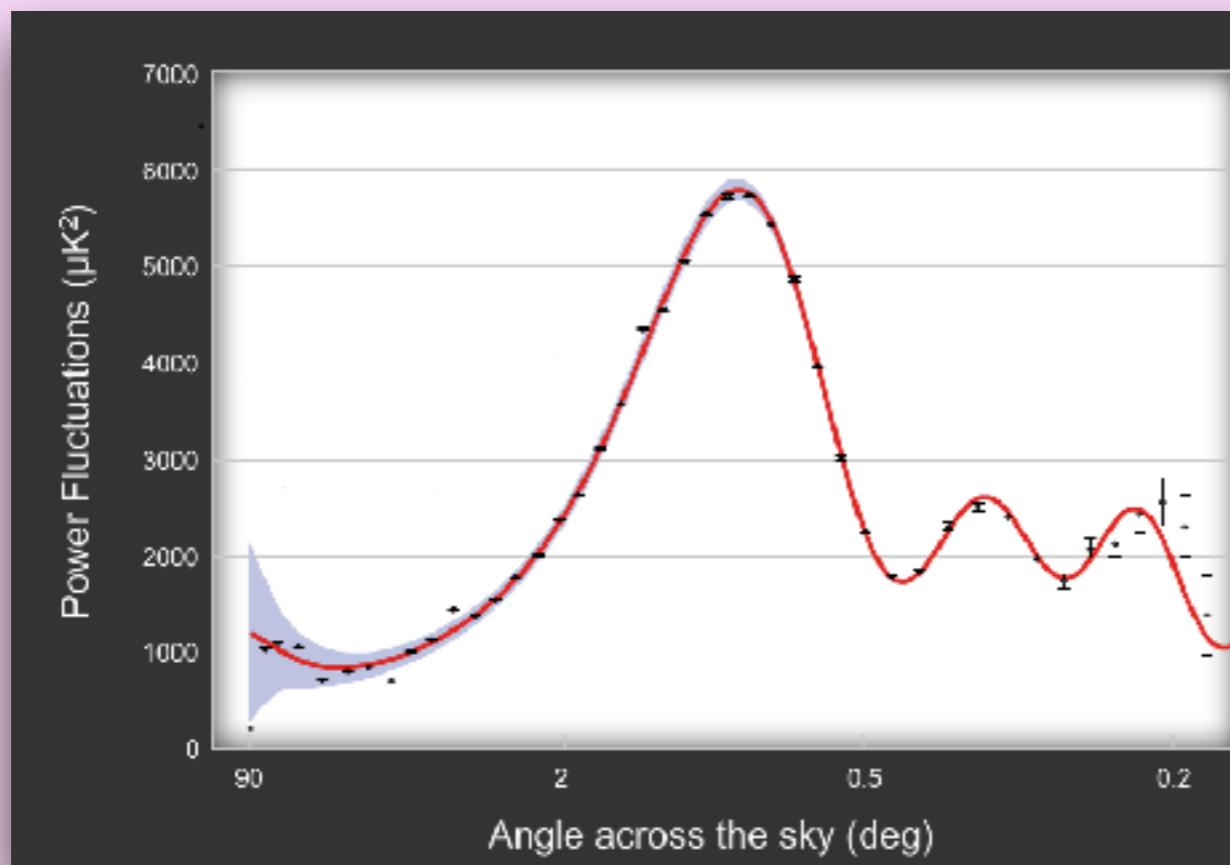
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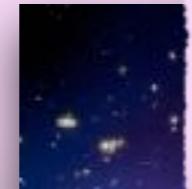


Cosmic Microwave Background



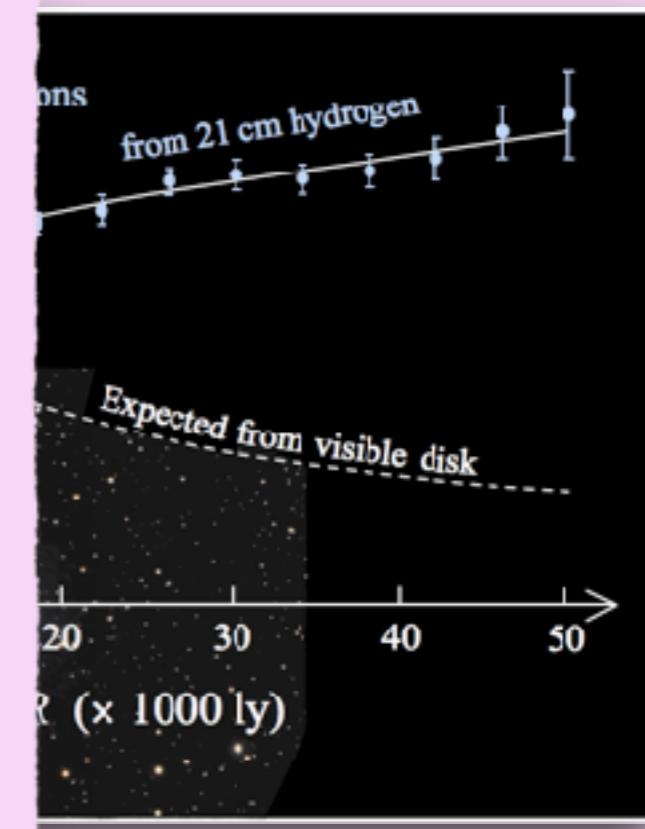
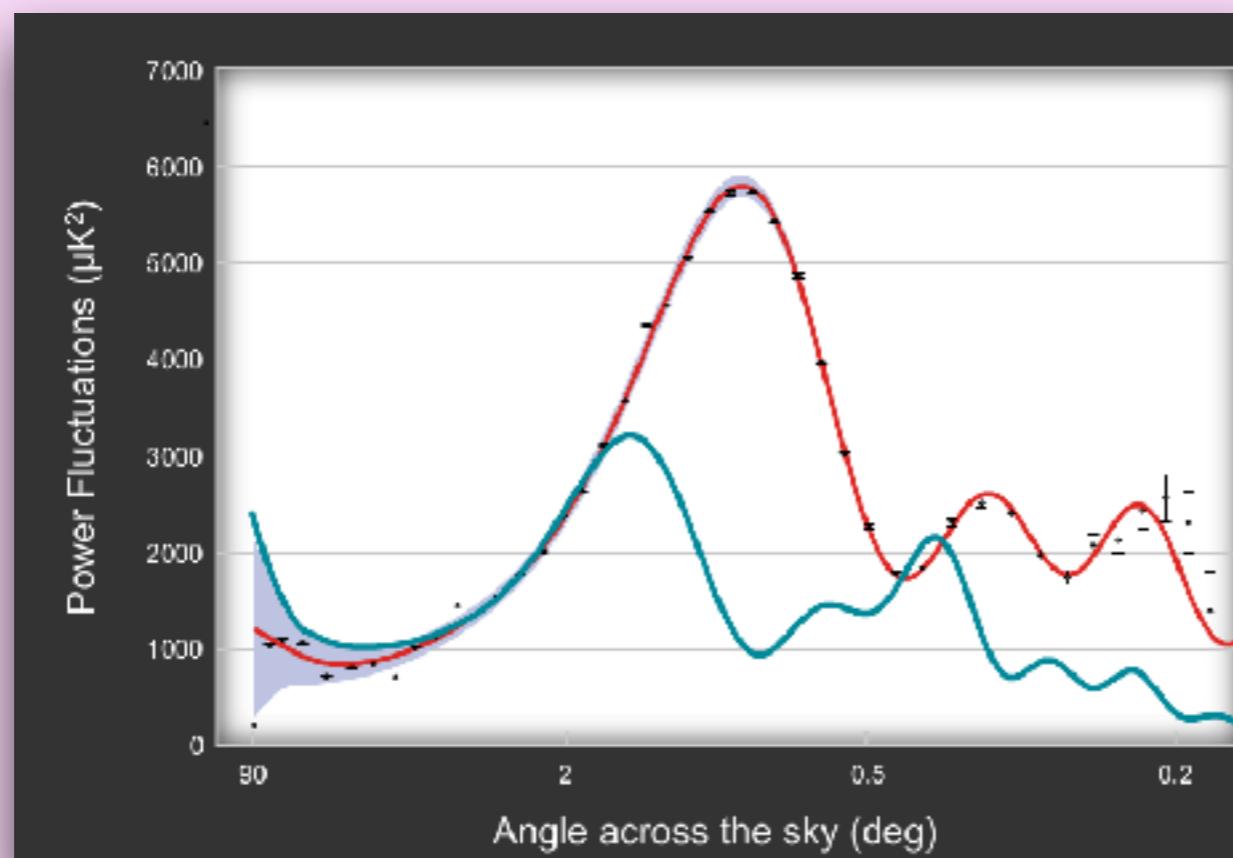
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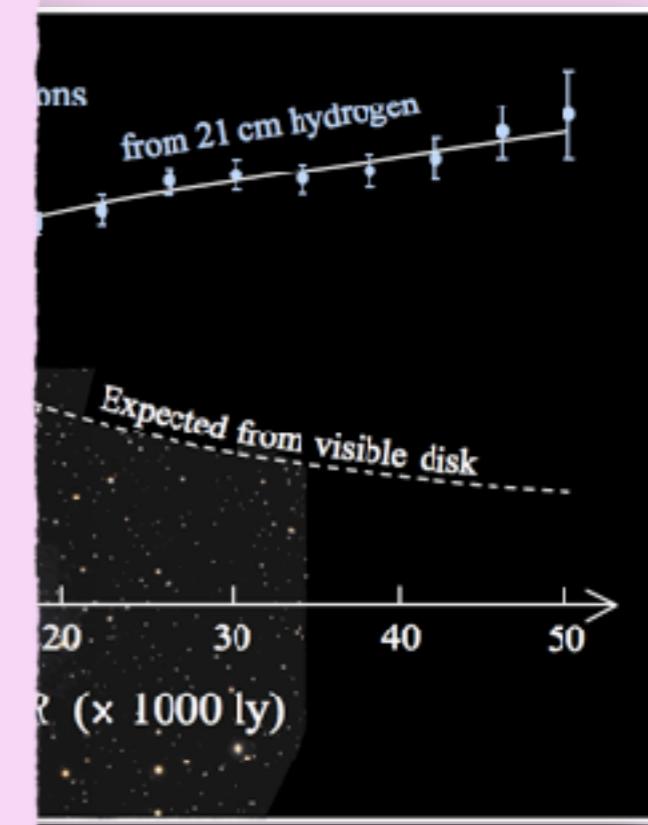
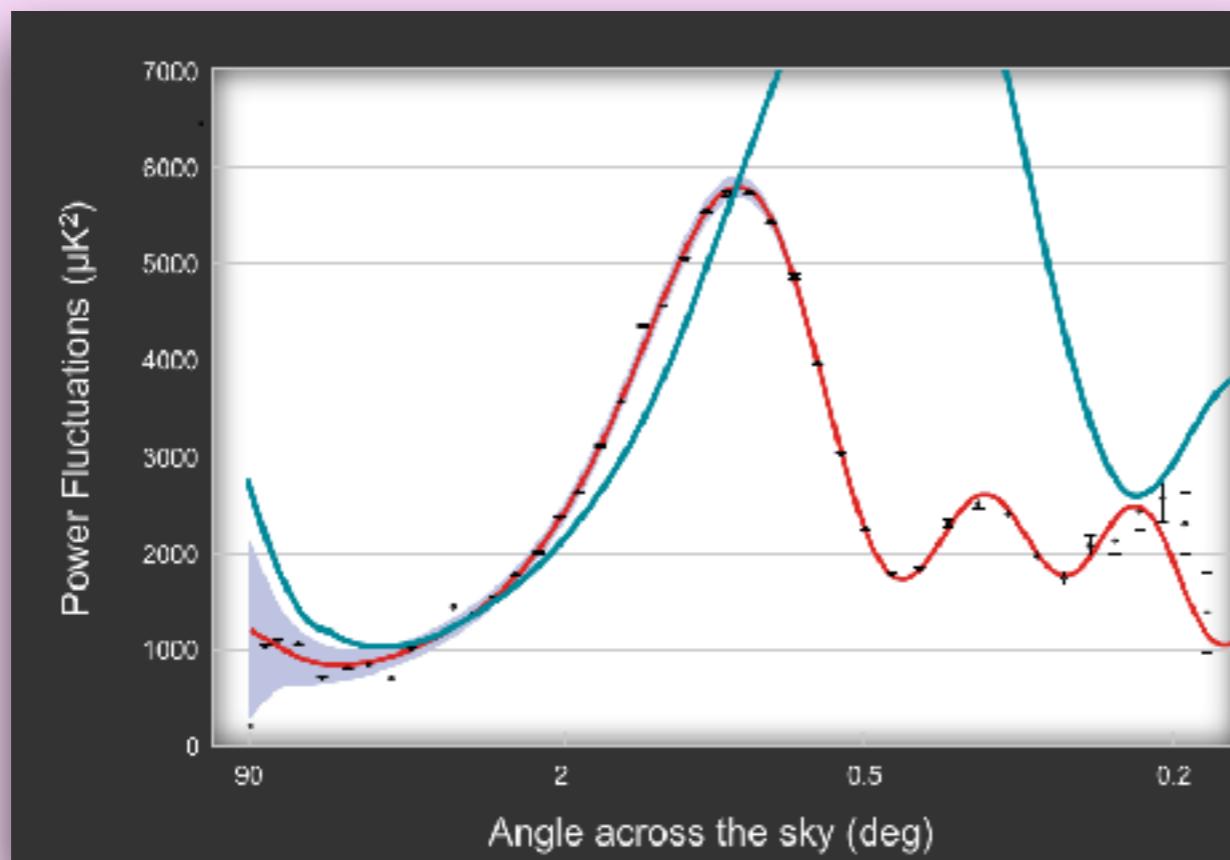
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Galaxy Clusters



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Cosmic Microwave Background



Standard Lore: Thermal Freeze-Out

- Early on: DM in thermal equilibrium with SM

e.g. via $\bar{\chi}\chi \longleftrightarrow \bar{f}f$

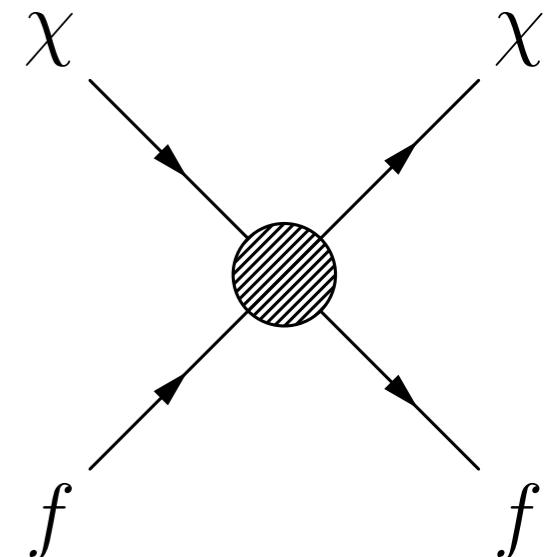
- Number density:

$$n_{\chi, \text{eq}} = \int \frac{d^3 p}{(2\pi)^3} \exp [-E_\chi(\vec{p})/T]$$

- T drops, interactions freeze out

- Described by Boltzmann equation

$$\frac{dn_\chi}{dt} + 3n_\chi \frac{\dot{a}}{a} = - \left(n_\chi^2 \langle \sigma(\chi\chi \rightarrow \bar{f}f) v_{\text{rel}} \rangle - n_f^2 \langle \sigma(\bar{f}f \rightarrow \chi\chi) v_{\text{rel}} \rangle \right)$$



Standard Lore: Thermal Freeze-Out

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- Detailed balance: $n_f^2 \langle \sigma(\bar{f}f \rightarrow \chi\chi) v_{\text{rel}} \rangle = n_{\chi,\text{eq}}^2 \langle \sigma(\chi\chi \rightarrow \bar{f}f) v_{\text{rel}} \rangle$
- Final Boltzmann equation

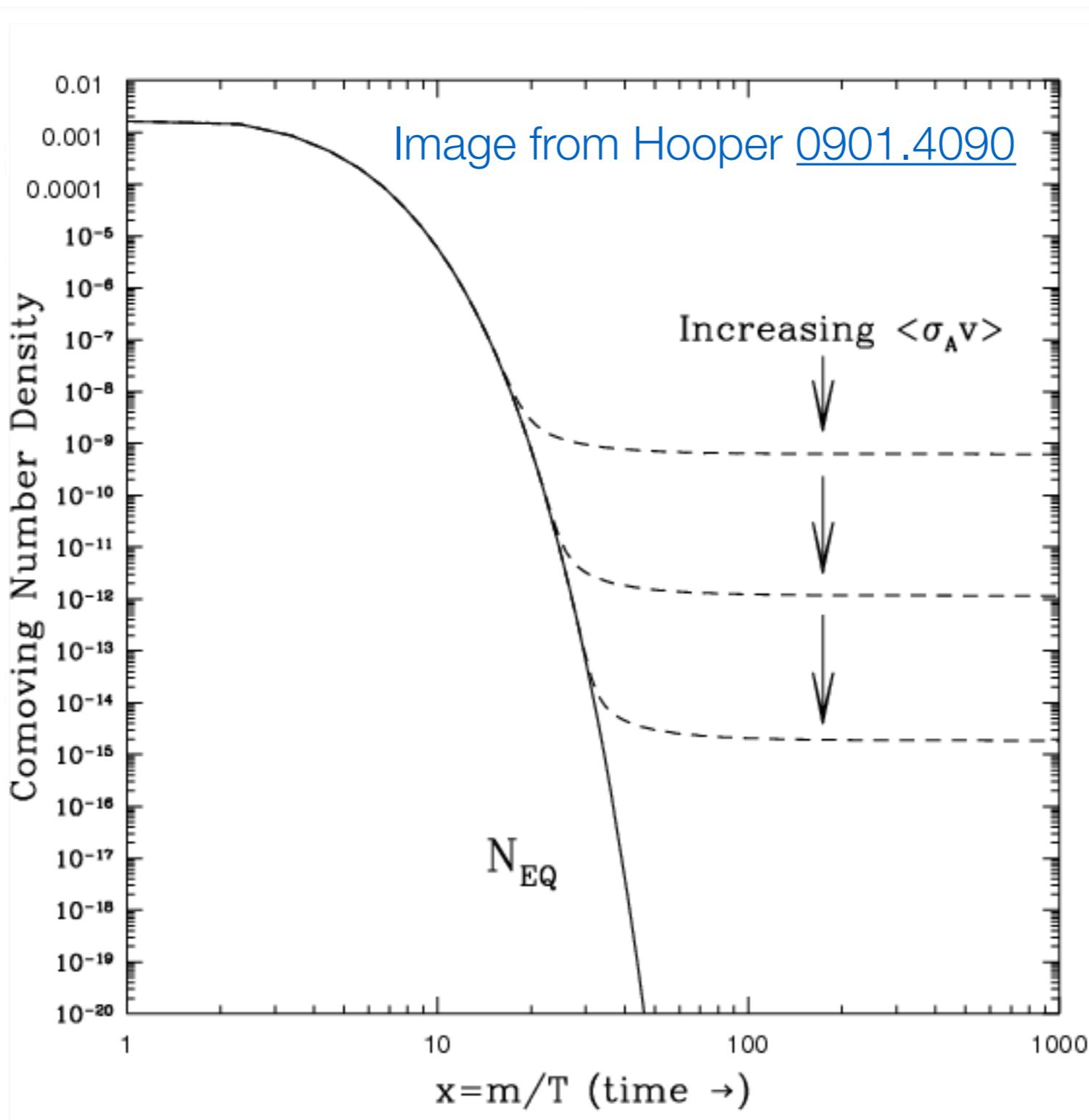
$$\frac{dn_\chi}{dt} + 3n_\chi \frac{\dot{a}}{a} = - \langle \sigma(\chi\chi \rightarrow \bar{f}f) v_{\text{rel}} \rangle (n_\chi^2 - n_{\chi,\text{eq}}^2)$$

Standard Lore: Thermal Freeze-Out

$$\frac{dn_\chi}{dt} + \dots$$

- Detailed
- Final Bo

$$\frac{dn_\chi}{dt} + \dots$$



$$\rightarrow \chi\chi)v_{rel}\rangle$$

$$\chi\chi \rightarrow \bar{f}f)v_{rel}\rangle$$

Standard Lore: Thermal Freeze-Out

$$\frac{dn_\chi}{dt} + \dots$$

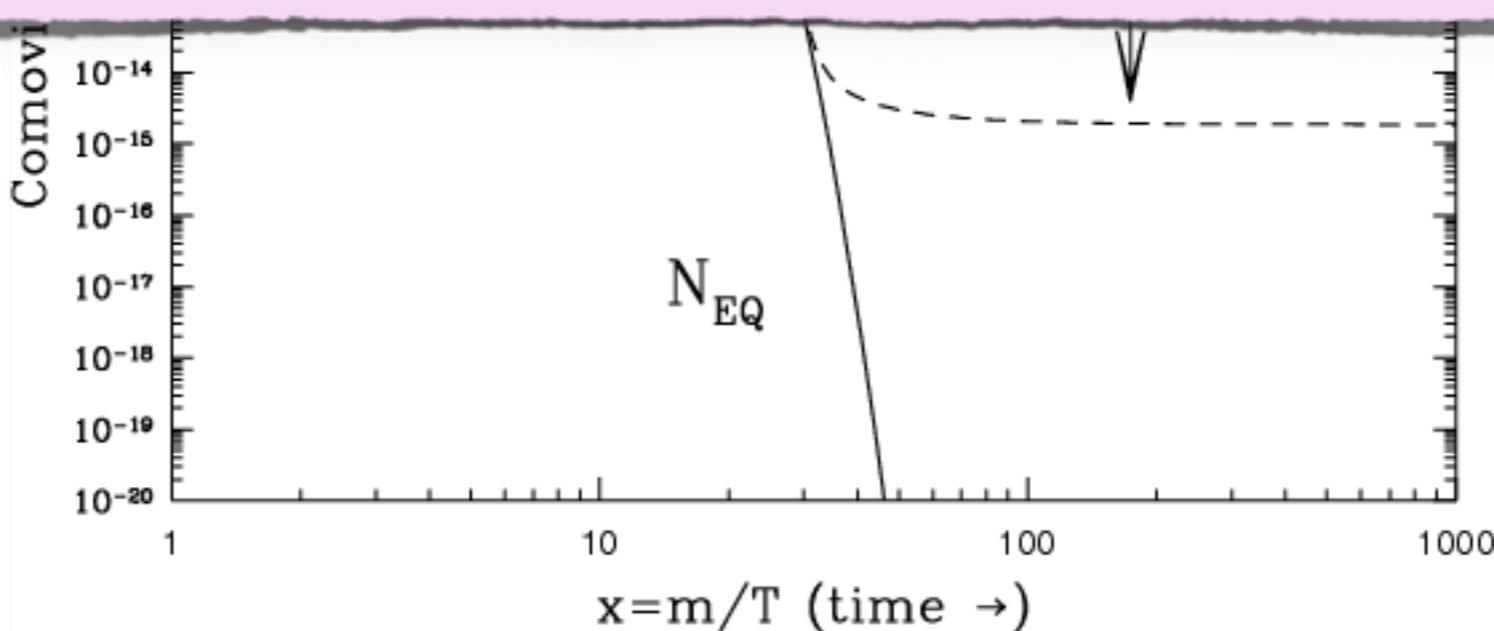


$$\rightarrow \chi\chi)v_{\text{rel}}\rangle$$

observed relic abundance obtained for

$$\langle\sigma(\chi\chi \rightarrow \bar{f}f)v_{\text{rel}}\rangle \simeq 2.2 \times 10^{-26} \text{ cm}^3/\text{sec}$$

$$\frac{dn_\chi}{dt} + \dots$$



Standard Lore: Thermal Freeze-Out

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$$\langle \sigma(\chi\chi \rightarrow \bar{f}f) v_{\text{rel}} \rangle \simeq 2.2 \times 10^{-26} \text{ cm}^3/\text{sec}$$

- Expect new particles at $\sim 100 \text{ GeV}$
- SM-like couplings $\sim \alpha_{\text{em}} \sim 0.01$
- Expect $\langle \sigma(\chi\chi \rightarrow \bar{f}f) v_{\text{rel}} \rangle \simeq \text{few} \times 10^{-26} \text{ cm}^3/\text{sec}$

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WIMP Miracle



Phase Transitions in the Early Universe

- Properties of the primordial plasma change dramatically during phase transitions
- Electroweak phase transition ($T \sim 160$ GeV)
 - Electroweak symmetry broken $SU(2)_L \times U(1)_Y \rightarrow U(1)_{\text{em}}$
 - Higgs acquires vev v_H , fermions and gauge bosons become massive
 - cross-over in the SM, but can be 1st or 2nd order in BSM models
 - order parameter: v_H
- QCD phase transition ($T \sim 200$ MeV)
 - chiral symmetry broken $SU(3)_L \times SU(3)_R \rightarrow SU(3)_V$
 - order parameter: $\langle q_L q_R \rangle$

Outline

- The Vev Flip-Flop: Temporarily Unstable Dark Matter**
- Kinematically Induced Freeze-In: Impact of Thermal Masses**
- Vev Flip-Flop Freeze-In: Switching Production Channels On/Off**
- Summary**

The Vev Flip-Flop

Temporarily Unstable Dark Matter



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Temporarily Unstable Dark Matter

Question: Impact of Phase Transitions on DM Physics?

Example:

- symmetry stabilizing DM is broken in phase transition
- DM partly decays
- 2nd phase transition restores symmetry

The Vev Flip-Flop

- Toy Model: SM + singlet scalar S

$$V^{\text{tree}} = -\mu_H^2 H^\dagger H + \lambda_H (H^\dagger H)^2 - \mu_S^2 S^\dagger S + \lambda_S (S^\dagger S)^2 + \lambda_p (H^\dagger H)(S^\dagger S)$$

- Typical behavior: 2-step phase transition

- High T : $\langle S \rangle = 0, \langle H \rangle = 0$

Profumo et al. [0705.2425](#)

Cline Laporte Yamashita Kraml [0905.2559](#)

- Intermediate T : $\langle S \rangle \neq 0, \langle H \rangle = 0$

Espinosa Konstandin Riva [1107.5441](#)

- Low T : $\langle S \rangle = 0, \langle H \rangle \neq 0$

Cui Randall Shuve [1106.4834](#),

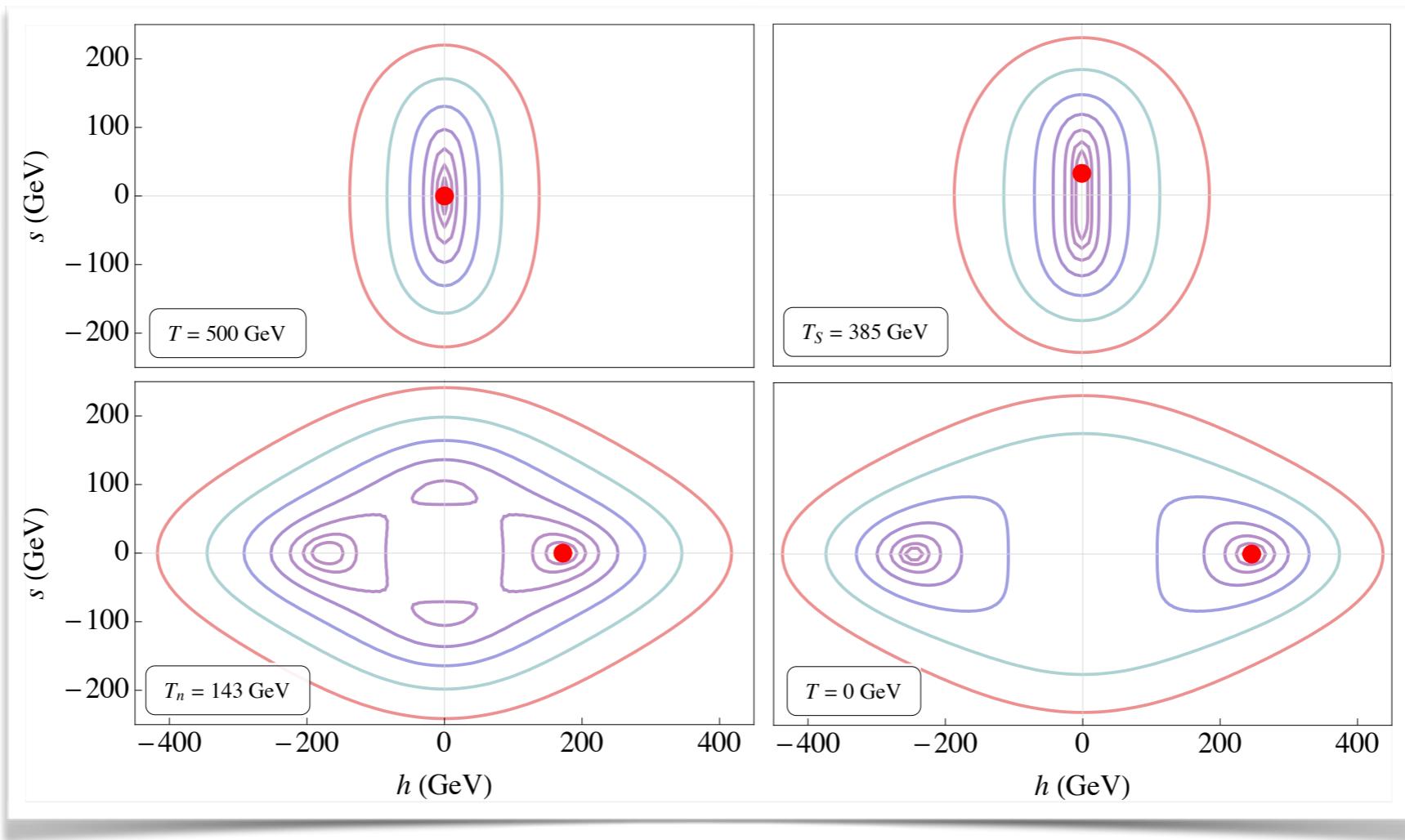
Cline Kainulainen [1210.4196](#)

Fairbairn Hogan [1305.3452](#)

Curtin Meade Yu [1409.0005](#)

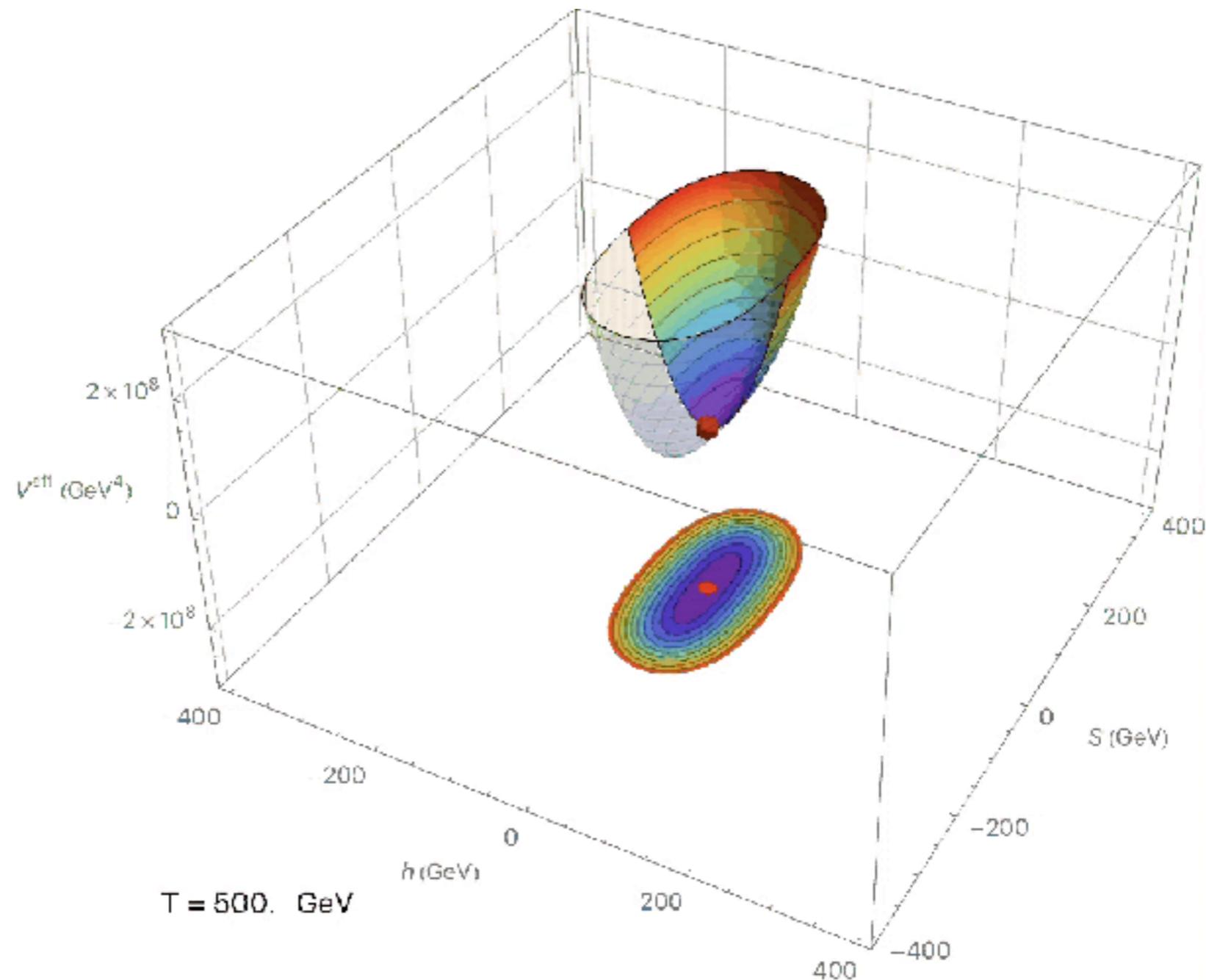
- Challenge: Make DM decay/annihilation rate $\propto \langle S \rangle$

The Vev Flip-Flop



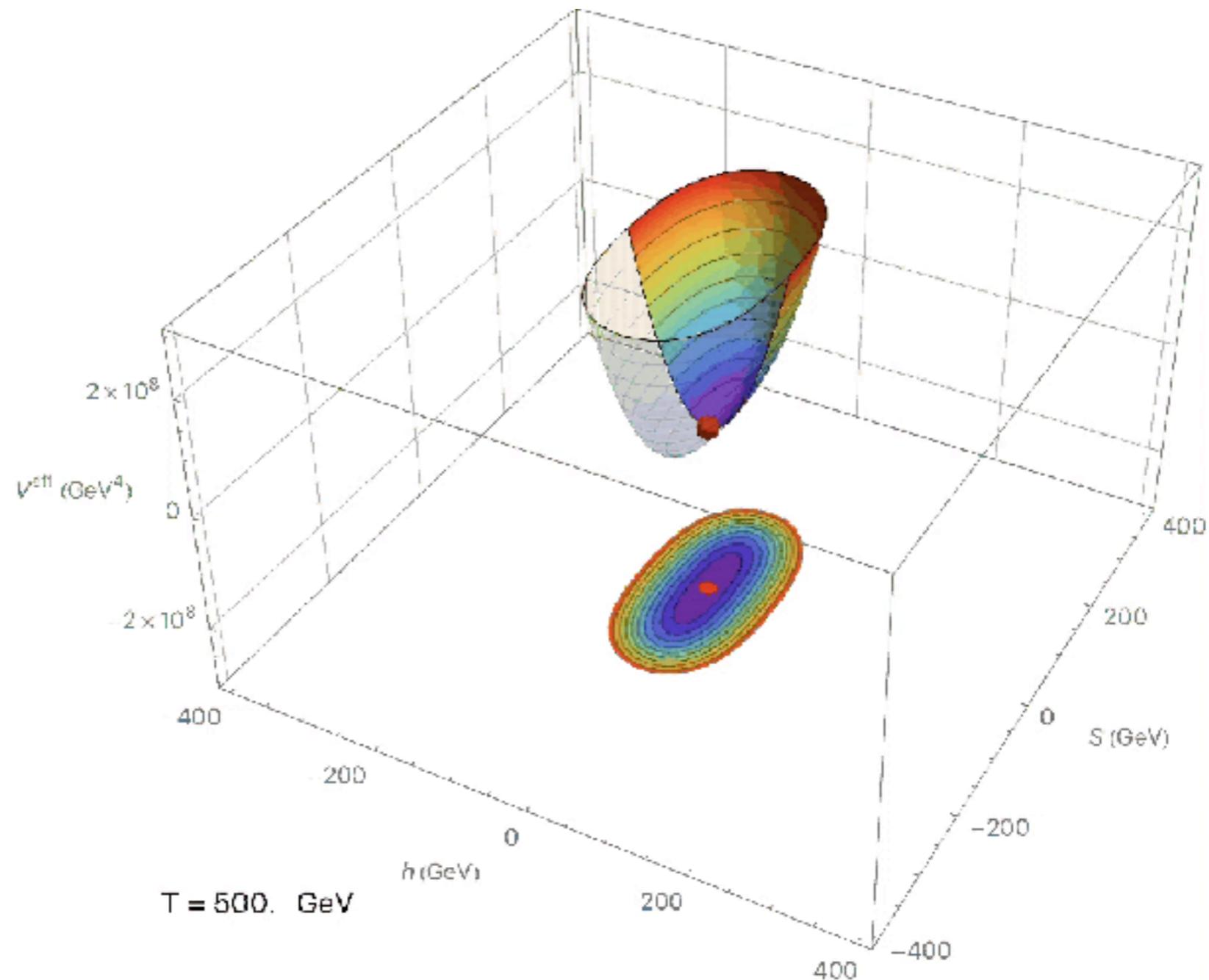
- $T > 400 \text{ GeV}$: $\langle S \rangle = 0$, $\langle H \rangle = 0$ (V_{eff} dominated by thermal corrections)
- $T \sim 400 \text{ GeV}$: S develops vev \rightarrow DM unstable
- $T \sim 150 \text{ GeV}$: H develops vev \rightarrow Feedback through $\lambda_p(H^\dagger H)(S^\dagger S)$
 $\rightarrow m_{S,\text{eff}}$ changes sign, $\langle S \rangle \rightarrow 0$, DM stable

The Vev Flip-Flop



Computed by Mike Baker using CosmoTransitions
Wainwright [1109.4189](#), Kozaczuk Profumo Haskins Wainwright [1407.4134](#)

The Vev Flip-Flop



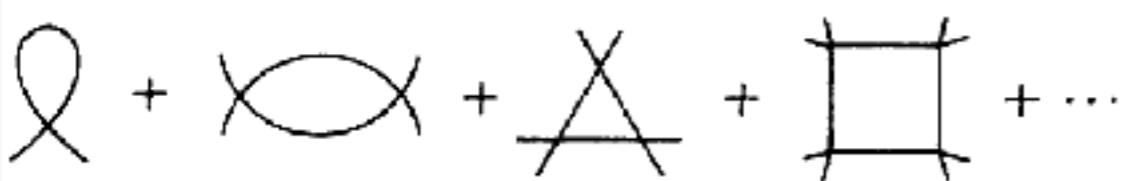
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Scalar Potentials at Finite Temperature

Tree level

$$V^{\text{tree}} = -\mu_H^2 H^\dagger H + \lambda_H (H^\dagger H)^2 - \mu_S^2 S^\dagger S + \lambda_S (S^\dagger S)^2 + \lambda_p (H^\dagger H)(S^\dagger S)$$

Coleman—Weinberg



[Coleman Weinberg 1973](#), [Dolan Jackiw 1974](#)

$$V^{\text{CW}}[\phi] = \sum_{n=1}^{\infty} \int \frac{d^4 k}{(2\pi)^4} \frac{1}{2n} \left(\frac{2\lambda\phi}{k^2 - m^2} \right)^n$$

- Sum over n
- Regularize, evaluate integral
- Renormalize by adding counterterms

$$V^{\text{CW}} = \sum_i \frac{n_i}{64\pi^2} m_i^4(h, S) \left[\log \frac{m_i^2(h, S)}{\Lambda^2} - \frac{3}{2} \right]$$

Scalar Potentials at Finite Temperature

1-loop finite T

[Dolan Jackiw 1974](#)

- Impose periodic boundary conditions on path integral

$$Z[J] = \exp\left[-\frac{1}{2} \int d^4x d^4y J(x) D(x-y) J(y)\right]$$

- Propagator (Green's function) at finite T is

$$D(x-y) = \frac{\text{tr}\left[e^{-\beta \hat{H}} T\phi(x)\phi(y)\right]}{\text{tr}\left[e^{-\beta \hat{H}}\right]}$$

evaluate by solving $(\partial_\mu \partial^\mu + m^2)D(x-y) = -i\delta^{(4)}(x-y)$ (periodic b.c.)

- 1-loop expansion of V_{eff} : $V^{(1)} = \frac{i}{2} \text{tr} \log D^{-1}$

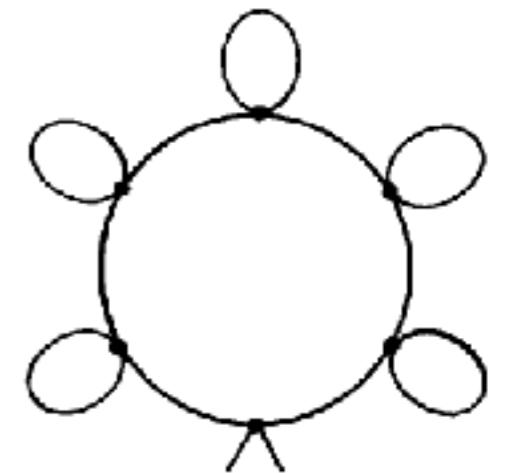
$$V^T = \sum_i \frac{n_i T^4}{2\pi^2} \int_0^\infty dx x^2 \log \left[1 \pm \exp \left(-\sqrt{x^2 + m_i^2(h, S)/T^2} \right) \right]$$

Scalar Potentials at Finite Temperature

Resummed “Daisy” Corrections [Dolan Jackiw 1974](#), [Carrington 1992](#)

- n one-vertex bubbles, one n -vertex bubble:

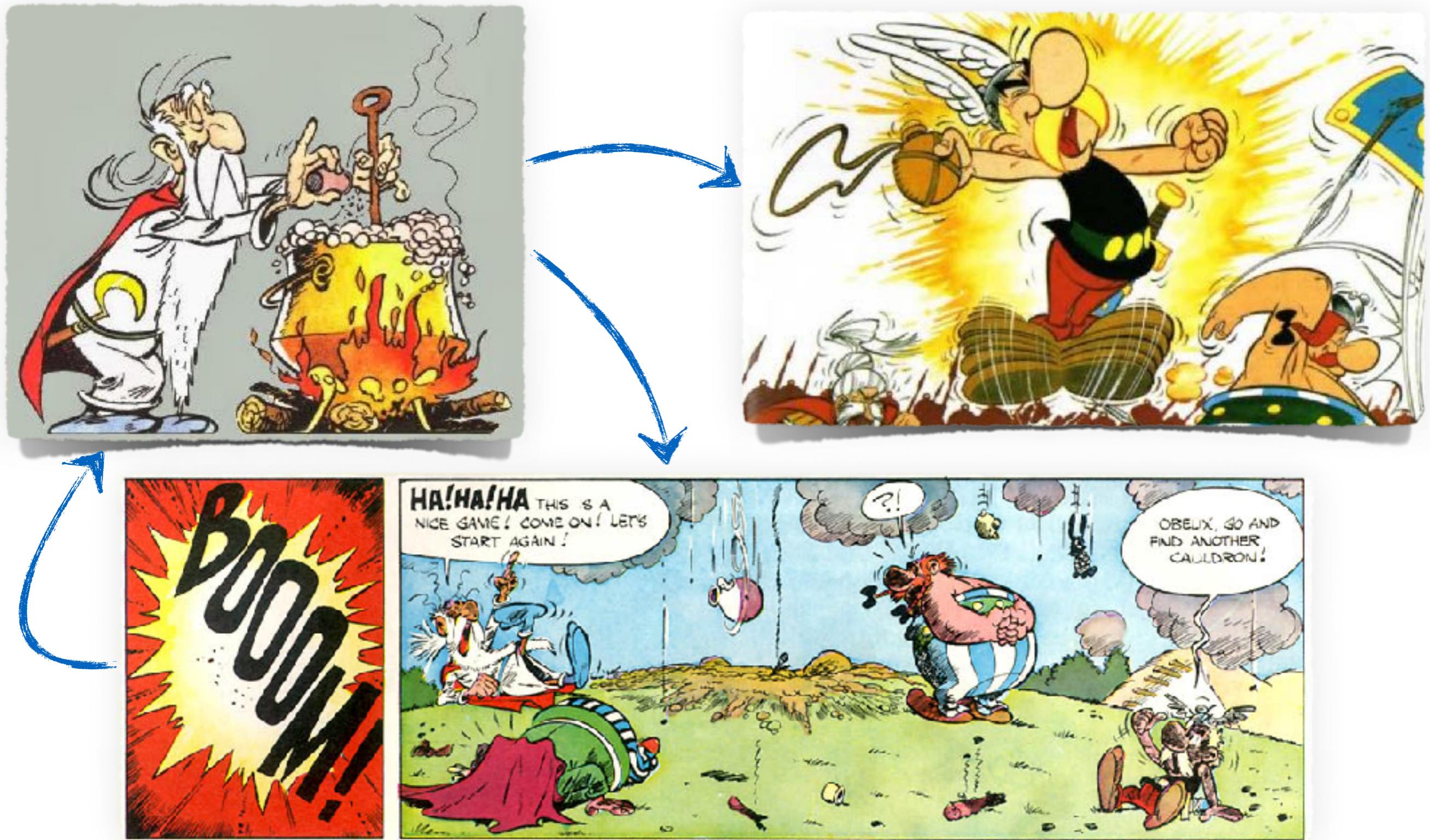
$$\sum_n \left(\int \frac{d^4 k}{(2\pi)^4} \tilde{D}(k) \right)^n \cdot \int \frac{d^4 k}{(2\pi)^4} (\tilde{D}(k))^n$$



- One-vertex bubbles yield thermal mass $\Pi(T)$

$$V^{\text{daisy}} = -\frac{T}{12\pi} \sum_i n_i \left([m_i^2(h, S) + \Pi_i(T)]^{\frac{3}{2}} - [m_i^2(h, S)]^{\frac{3}{2}} \right)$$

Dark Matter Model Building Flowchart



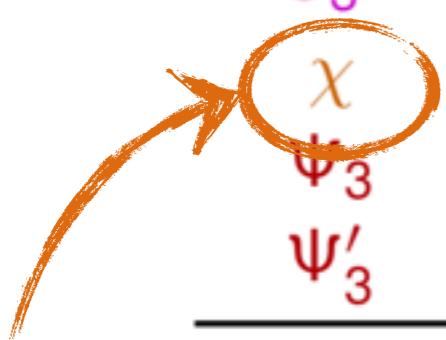
A Toy Model

Field	Spin	SM	\mathbb{Z}_3	mass scale
S_3	0	(1, 3, 0)	$S_3 \rightarrow e^{2\pi i/3} S_3$	100 GeV
χ	$\frac{1}{2}$	(1, 1, 0)	$\chi \rightarrow e^{2\pi i/3} \chi$	TeV
Ψ_3	$\frac{1}{2}$	(1, 3, 0)	$\Psi_3 \rightarrow e^{-2\pi i/3} \Psi_3$	TeV
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Baker JK [1608.07578](#)

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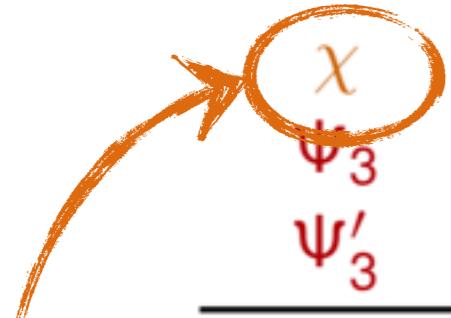
DM candidate

Baker JK [1608.07578](#)

A Toy Model

stabilizes DM

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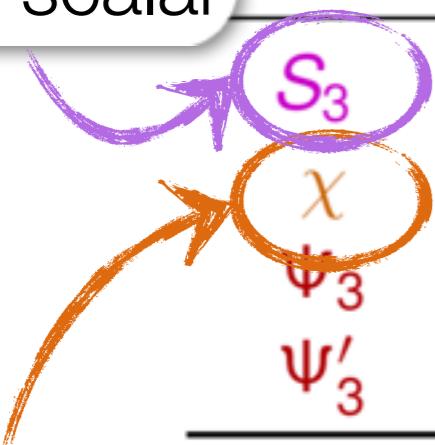


Baker JK [1608.07578](#)

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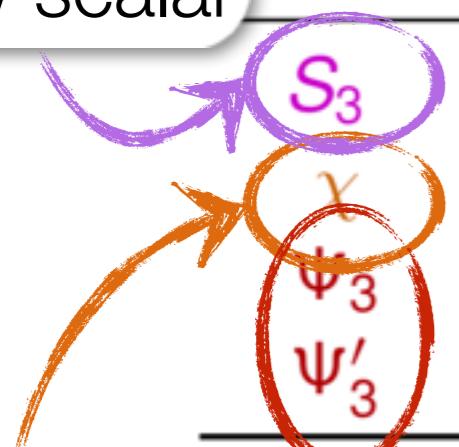
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DM candidate

DM decay products

Baker JK [1608.07578](#)

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stabilizes DM

DM candidate

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Baker JK [1608.07578](#)

$$\mathcal{L} \supset y_\chi S_3^\dagger \bar{\chi} \Psi_3 + y'_\chi S_3^\dagger \bar{\chi} \Psi'_3 + y_\Psi \epsilon^{ijk} S_3^i \bar{\Psi}_3^j (\Psi'_3)^k + h.c.$$

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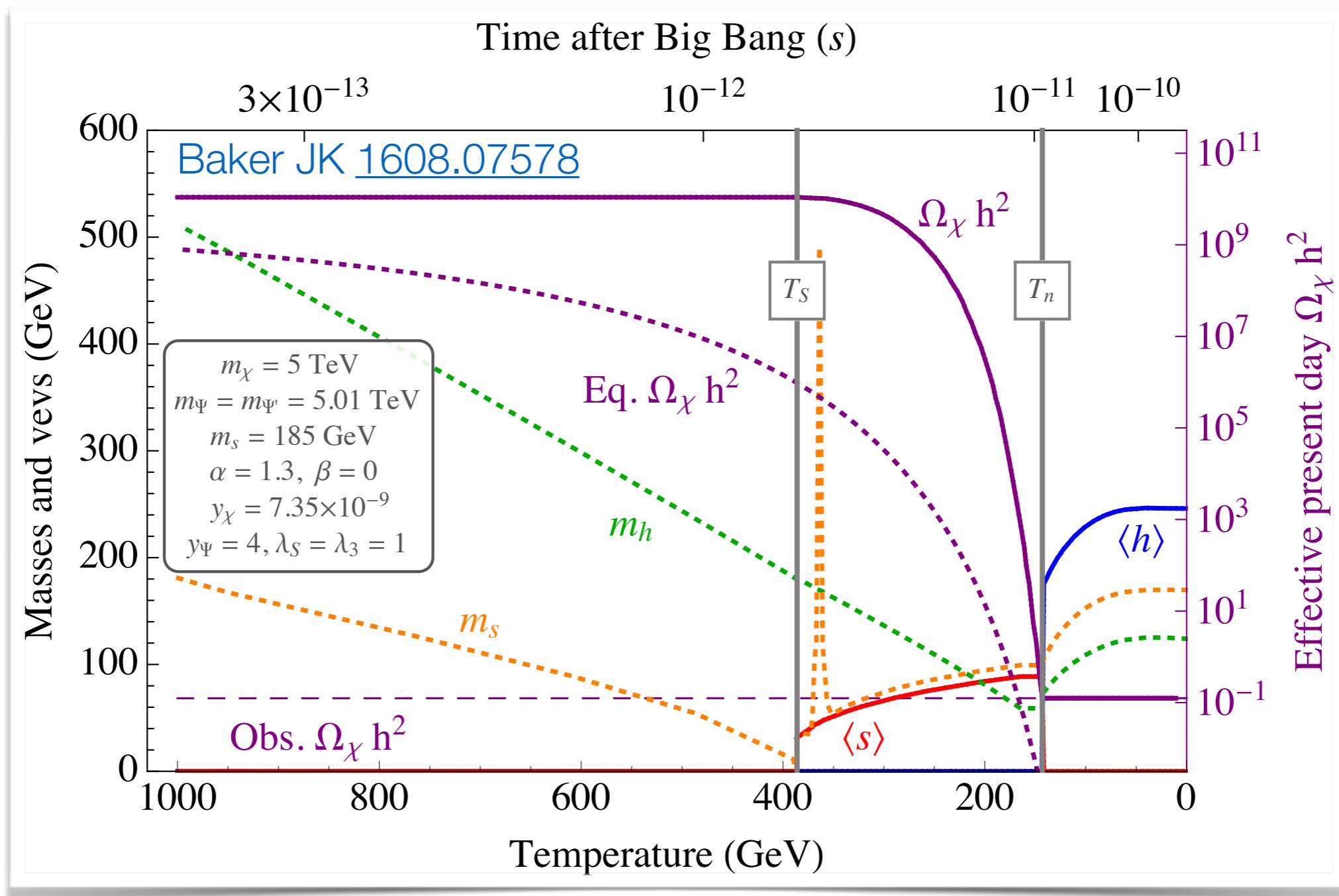
stabilizes DM

DM candidate DM decay products Baker JK [1608.07578](#)

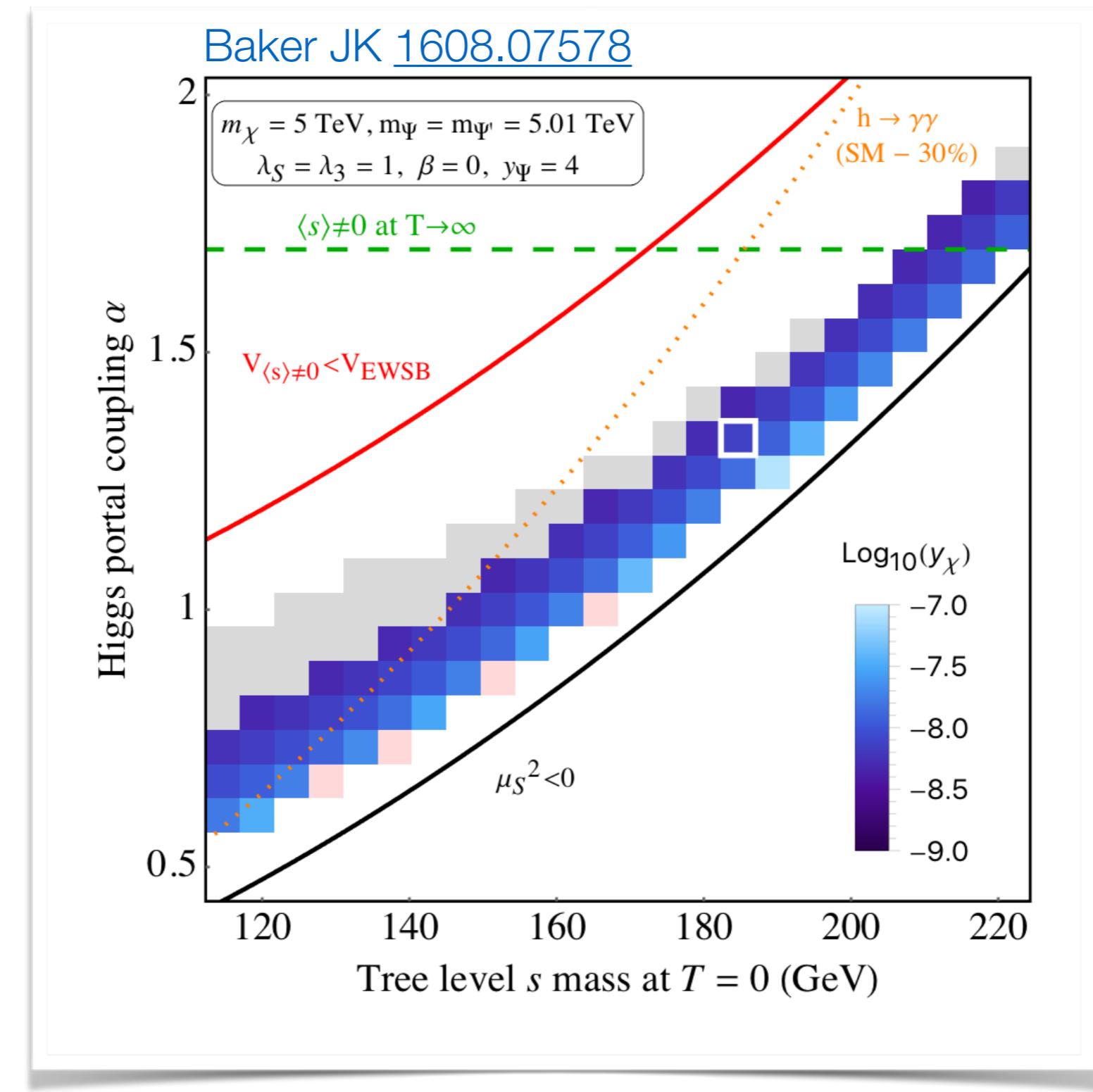
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- $\langle S \rangle$ leads to mixing between χ , Ψ_3 , Ψ'_3 alters Ψ_3 , Ψ'_3 masses
- χ decays via $\chi \rightarrow W\Psi_3$, $S\Psi_3$ when $\langle S \rangle \neq 0$

Cosmological Evolution

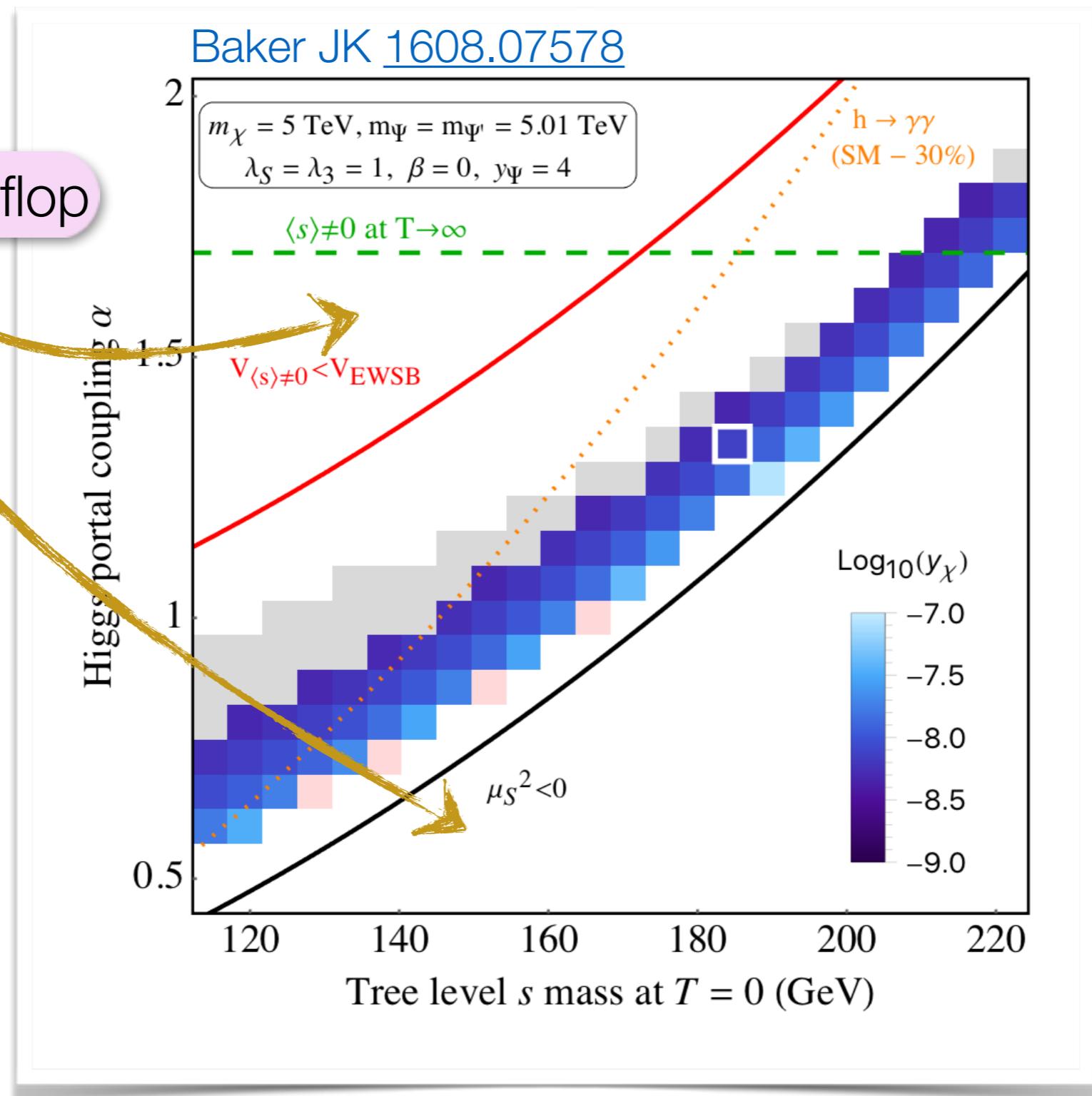


Parameter Space



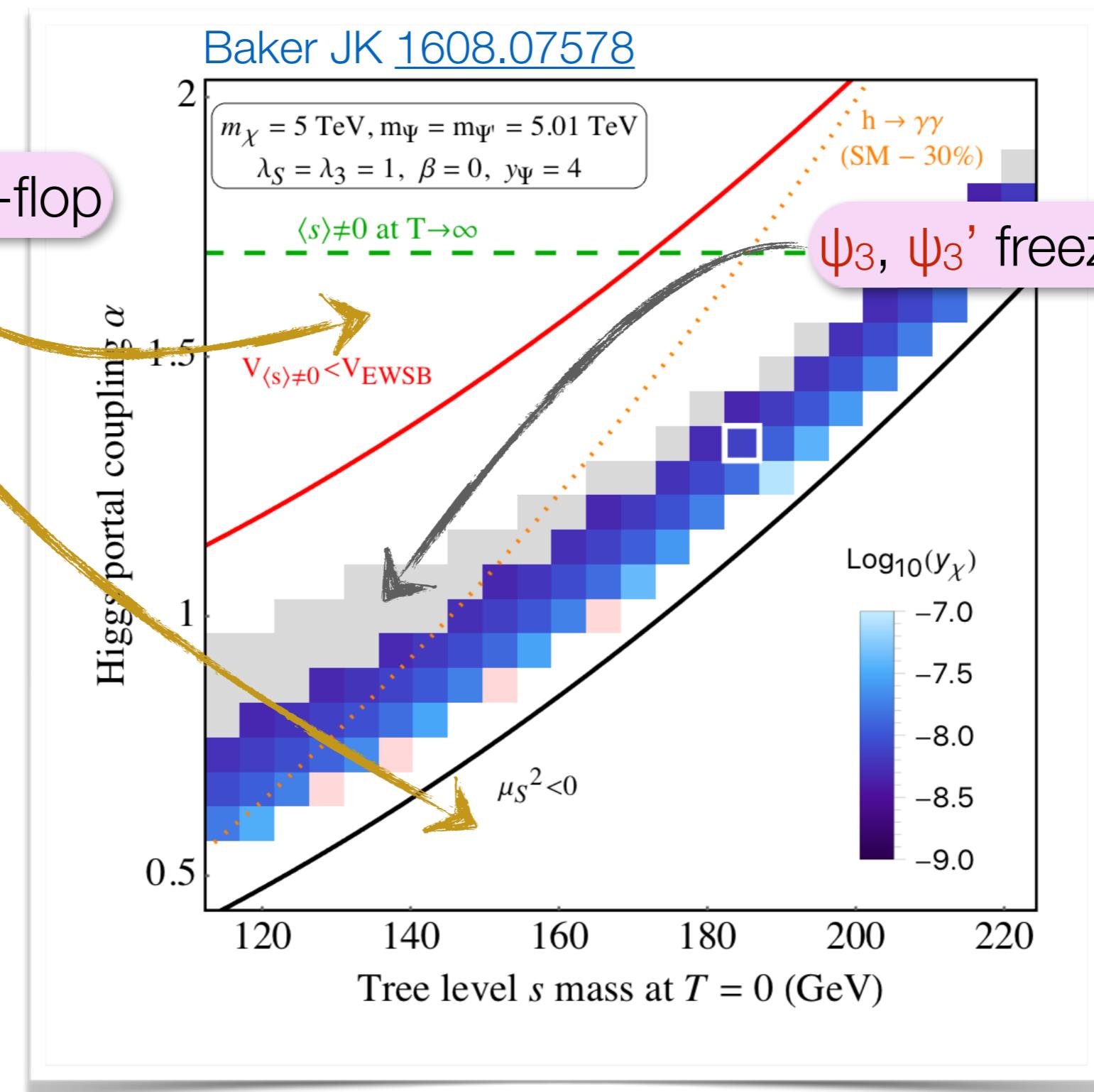
Parameter Space

no vev flip-flop



Parameter Space

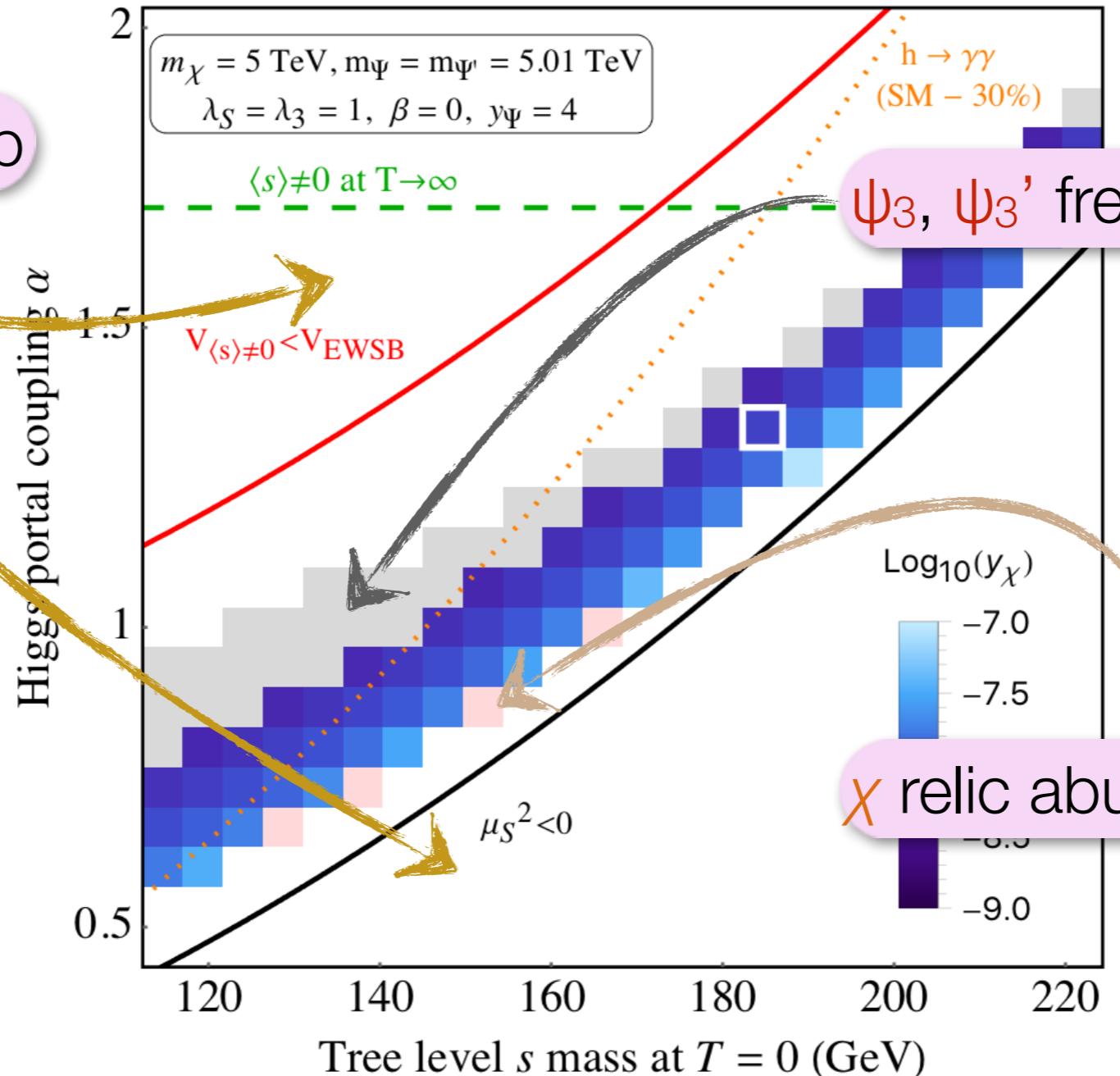
no vev flip-flop



Parameter Space

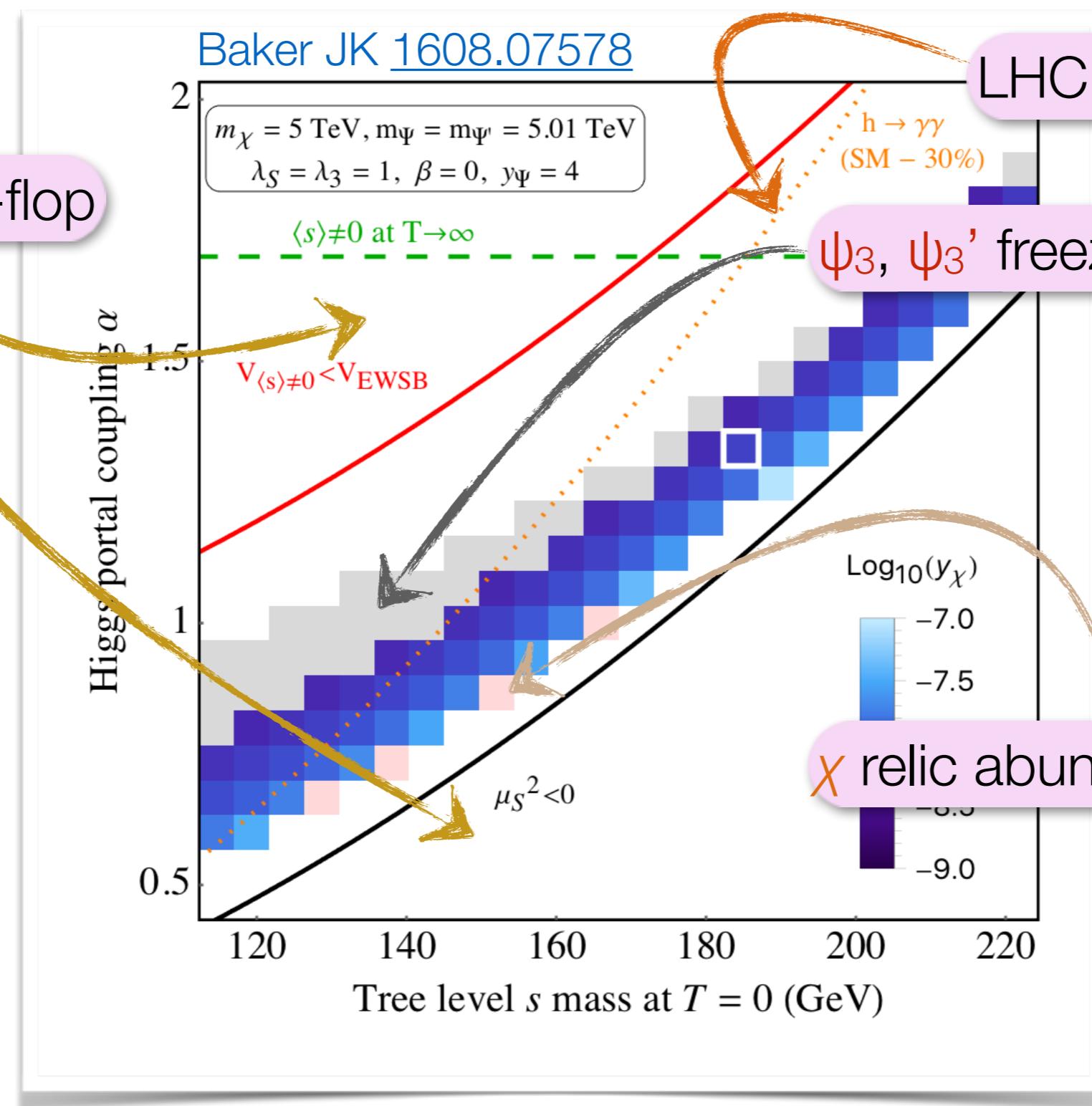
no vev flip-flop

Baker JK [1608.07578](#)



Parameter Space

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Thermal Effects in DM Freeze-In



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DM Freeze-In in Higgs Portal Models

Toy Model: SM + singlet scalar S + DM fermion χ + fermion ψ

$$\begin{aligned}\mathcal{L} \supset & \frac{1}{2}(\partial_\mu S)(\partial^\mu S) + \bar{\psi}(i\cancel{D} - m_\psi)\psi + \bar{\chi}(i\cancel{D} - m_\chi)\chi \\ & + [y_{\psi\chi} \bar{\psi}S\chi + h.c.] + y_\chi \bar{\chi}\chi S + y_\psi \bar{\psi}\psi S - V(H, S)\end{aligned}$$

Scalar Potential:

$$\begin{aligned}V(H, S) = & -\mu_H^2 H^\dagger H + \lambda_{H4} (H^\dagger H)^2 - \frac{1}{2} \mu_S^2 S^2 + \frac{\lambda_{S4}}{4!} S^4 \\ & + \frac{\lambda_{S3}}{3!} \mu_S S^3 + \lambda_{p3} \mu_S S (H^\dagger H) + \frac{\lambda_{p4}}{2} S^2 (H^\dagger H).\end{aligned}$$

Baker Breitbach JK Mittnacht [1712.03962](https://jkmittnacht.com)

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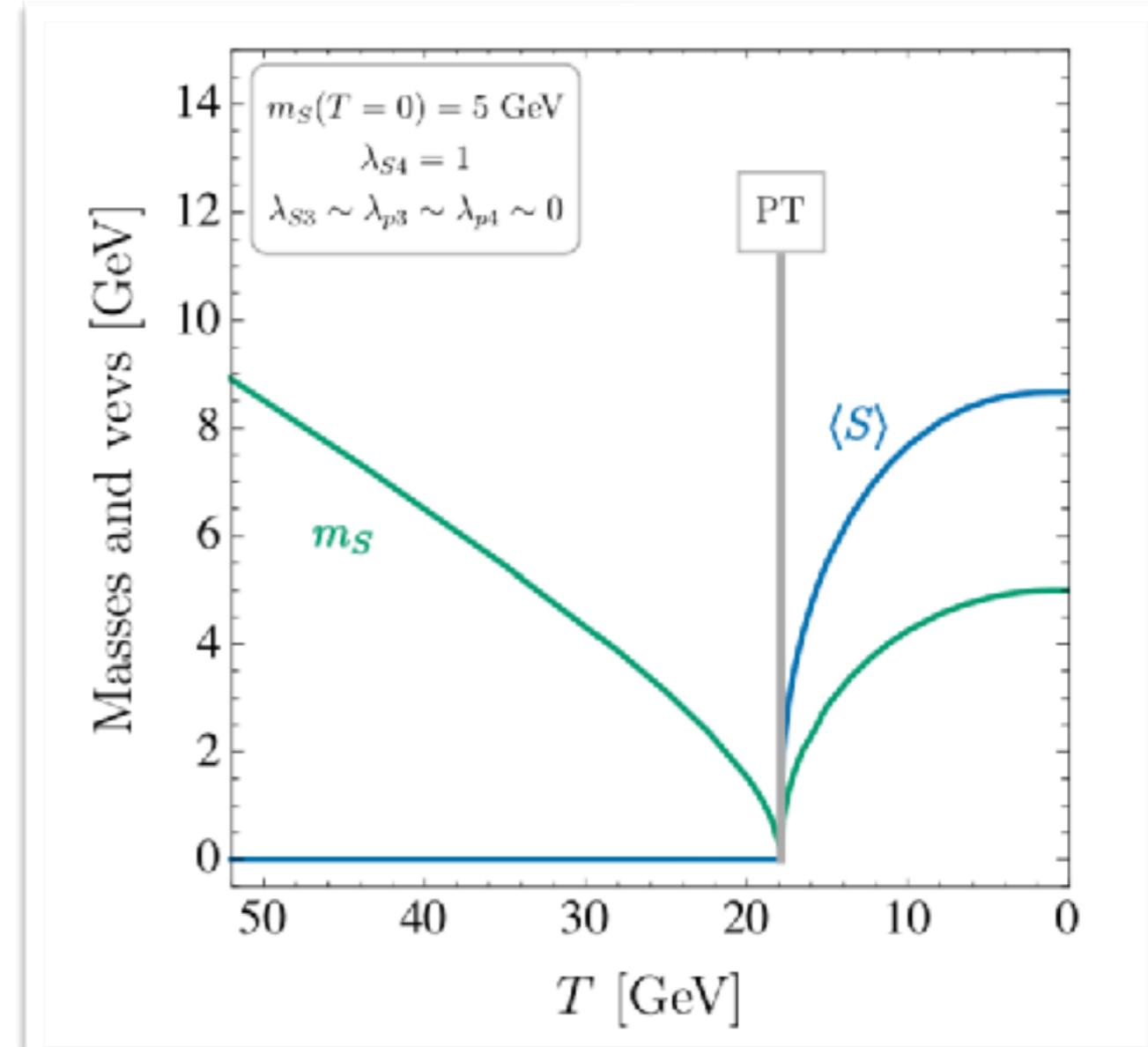
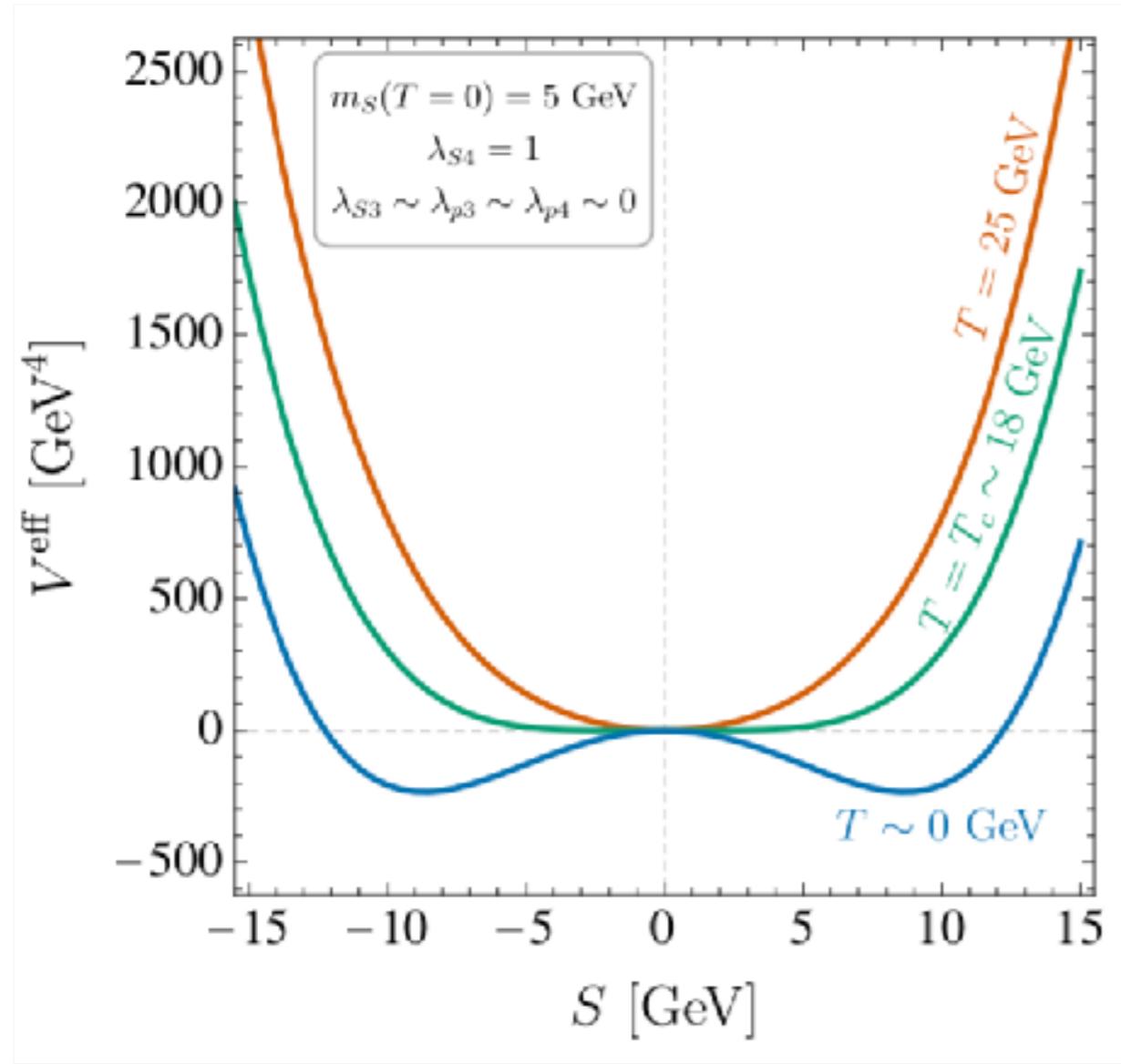
Scalar Potential:

$$\begin{aligned}V(H, S) = & -\mu_H^2 H^\dagger H + \lambda_{H4} (H^\dagger H)^2 - \frac{1}{2} \mu_S^2 S^2 + \frac{\lambda_{S4}}{4!} S^4 \\ & + \frac{\lambda_{S3}}{3!} \mu_S S^3 + \lambda_{p3} \mu_S S (H^\dagger H) + \frac{\lambda_{p4}}{2} S^2 (H^\dagger H).\end{aligned}$$

assumed small

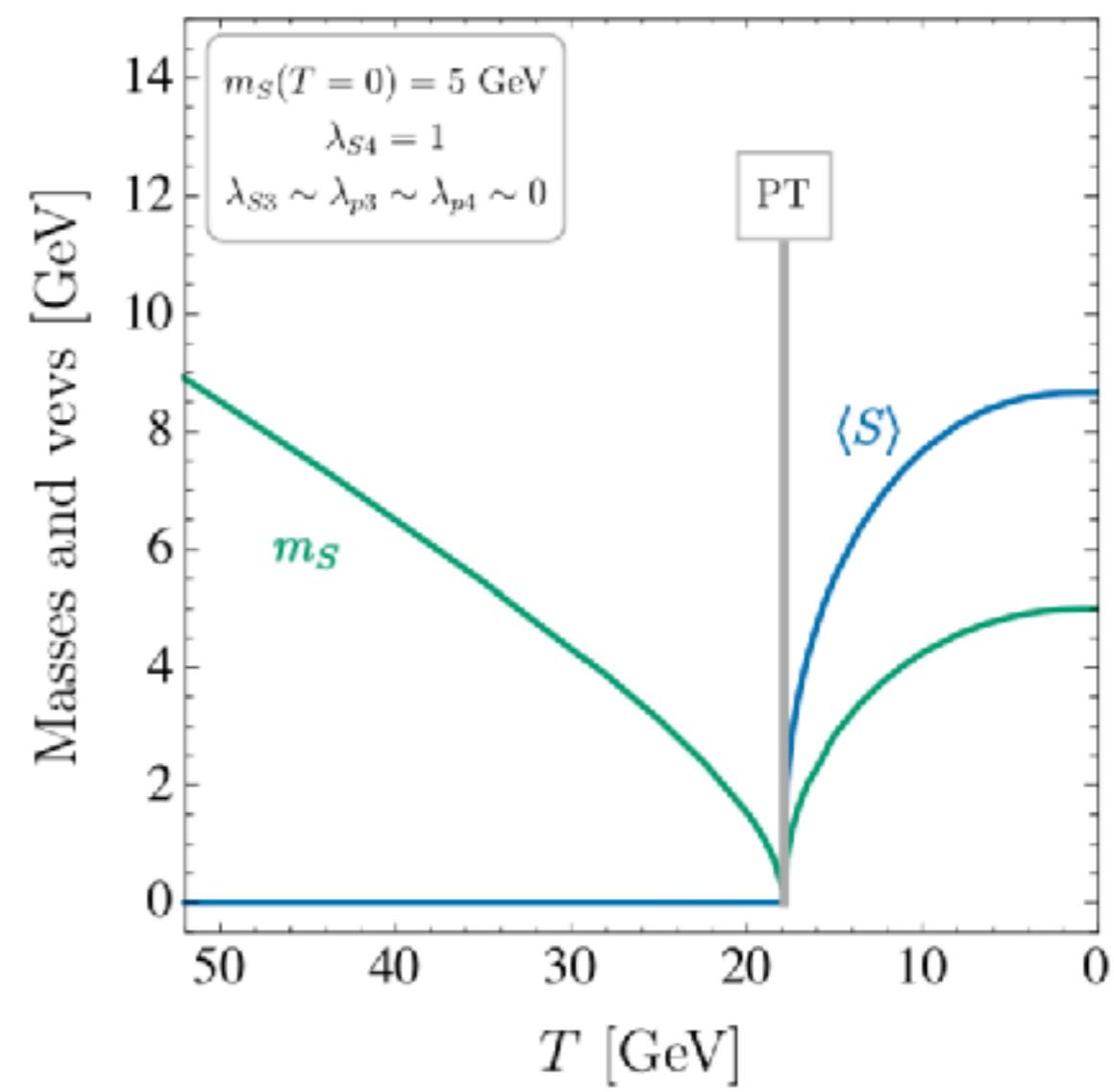
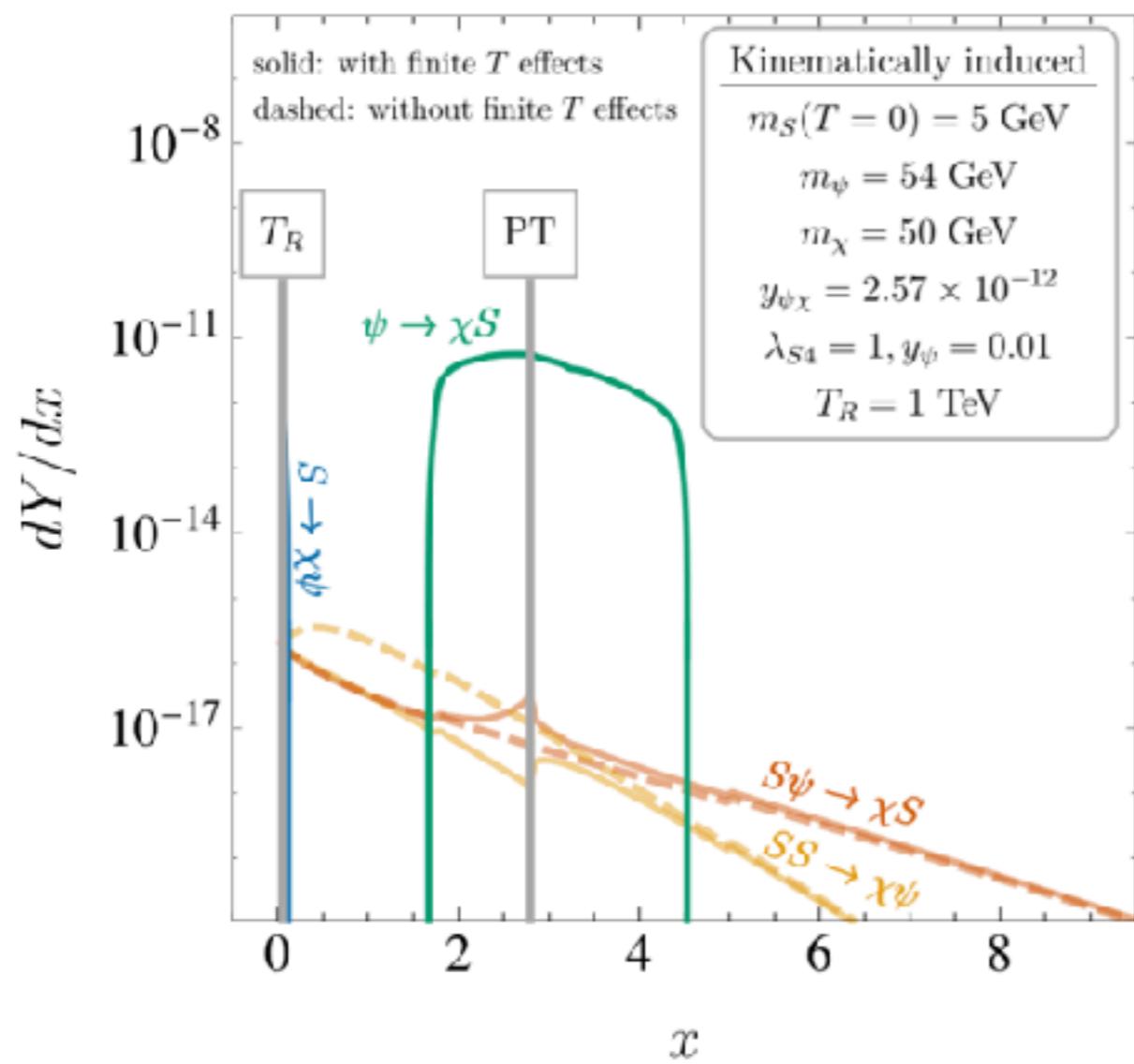
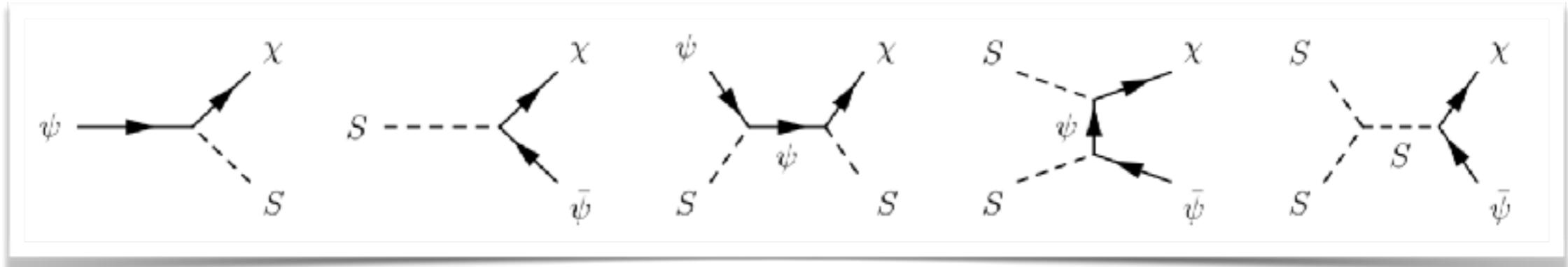
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Effective Potential and Thermal Masses

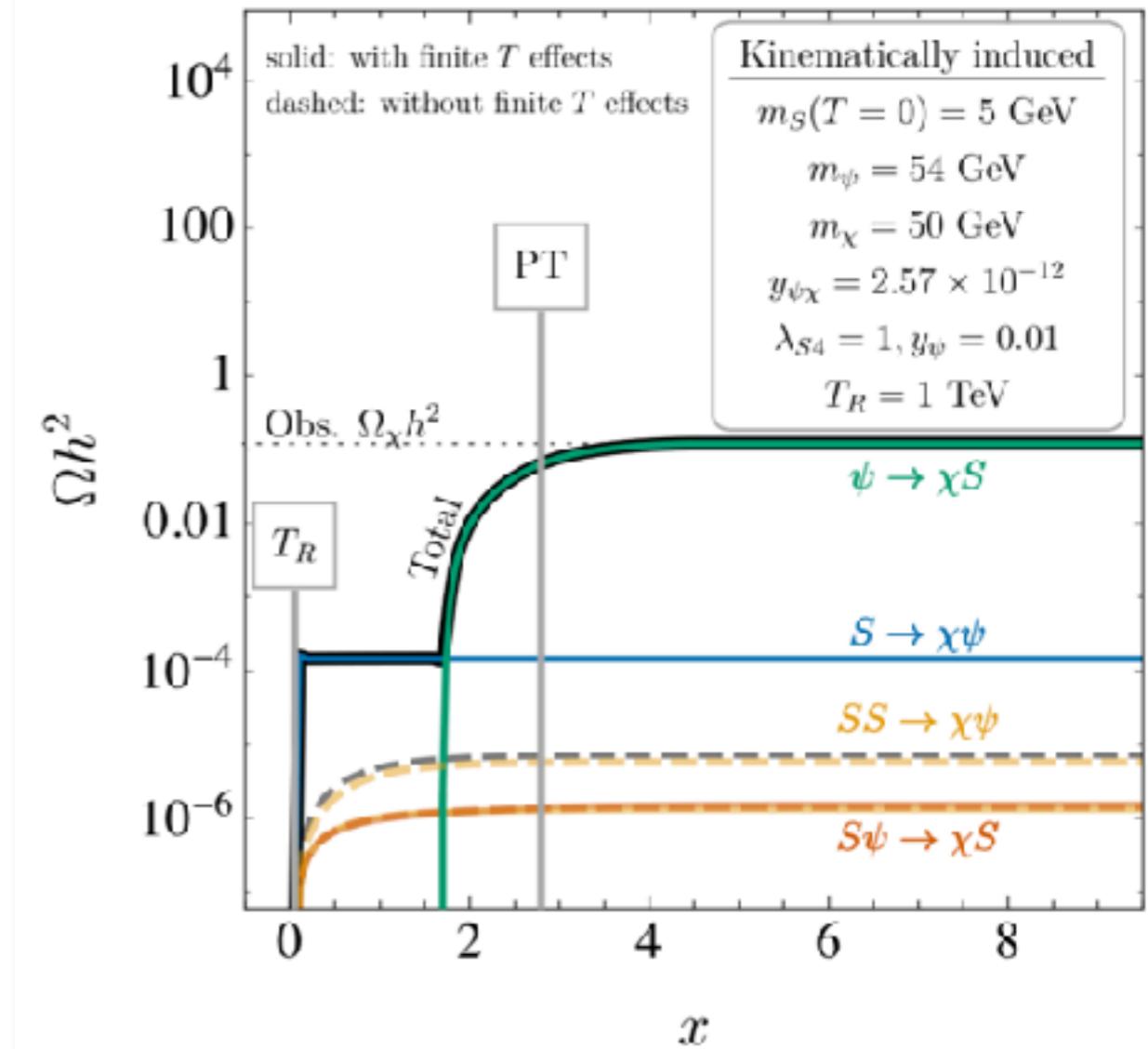
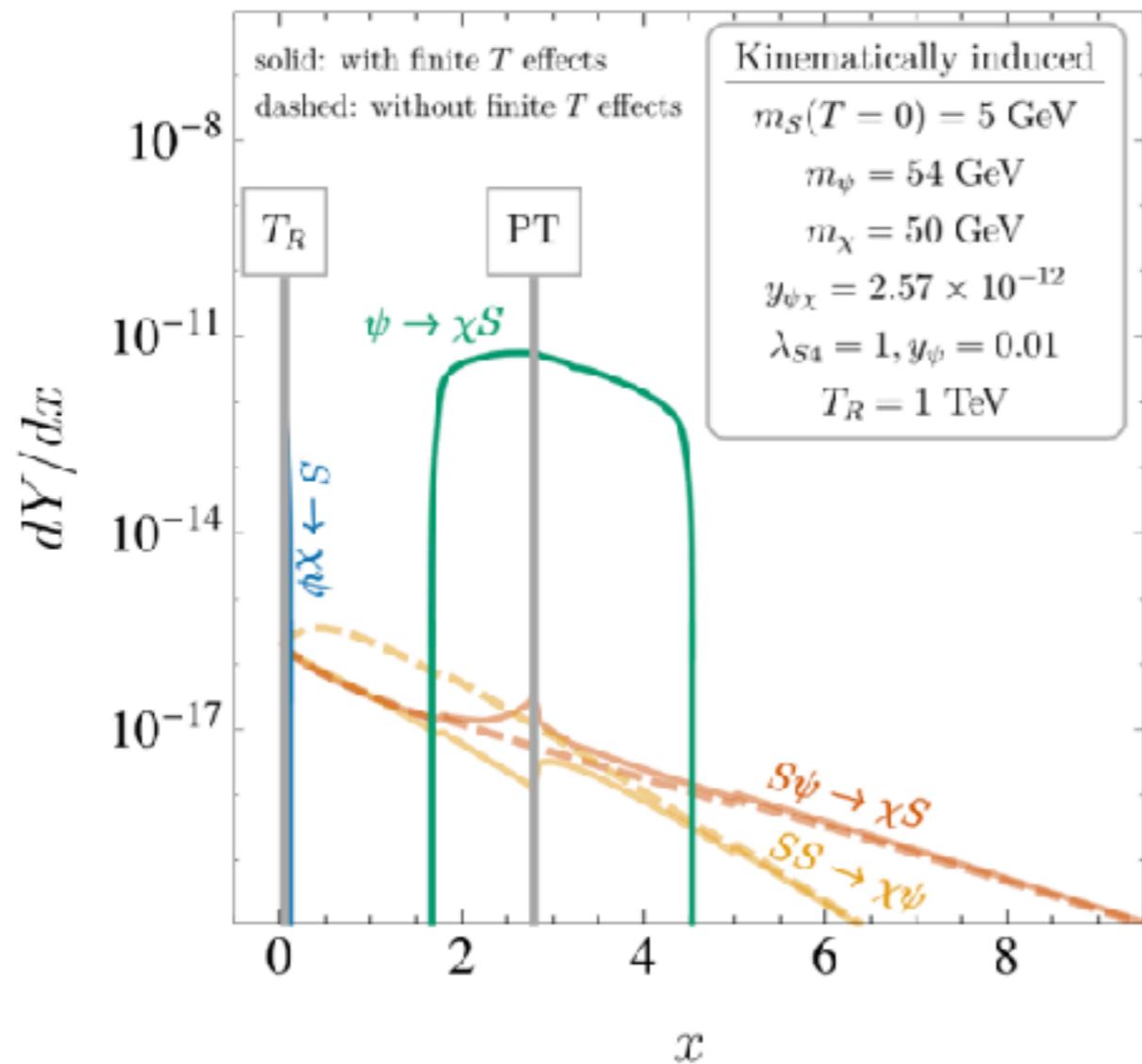
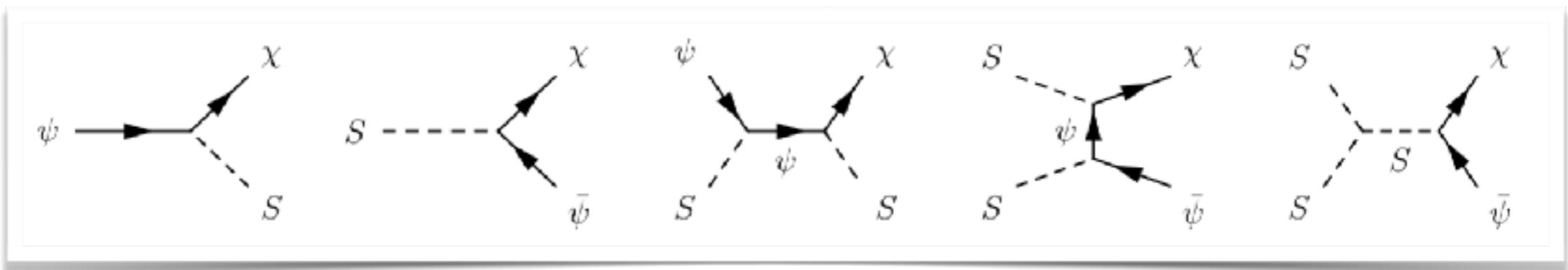


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DM Freeze-In



DM Freeze-In



Variation: Vev Flip-Flop Freeze-In

Toy Model: SM + singlet scalar S + DM fermion χ

$$\mathcal{L} \supset \frac{1}{2}(\partial_\mu S)(\partial^\mu S) + \bar{\chi}(i\cancel{D} - m_\chi)\chi + y_\chi \bar{\chi}\chi S - V(H, S)$$

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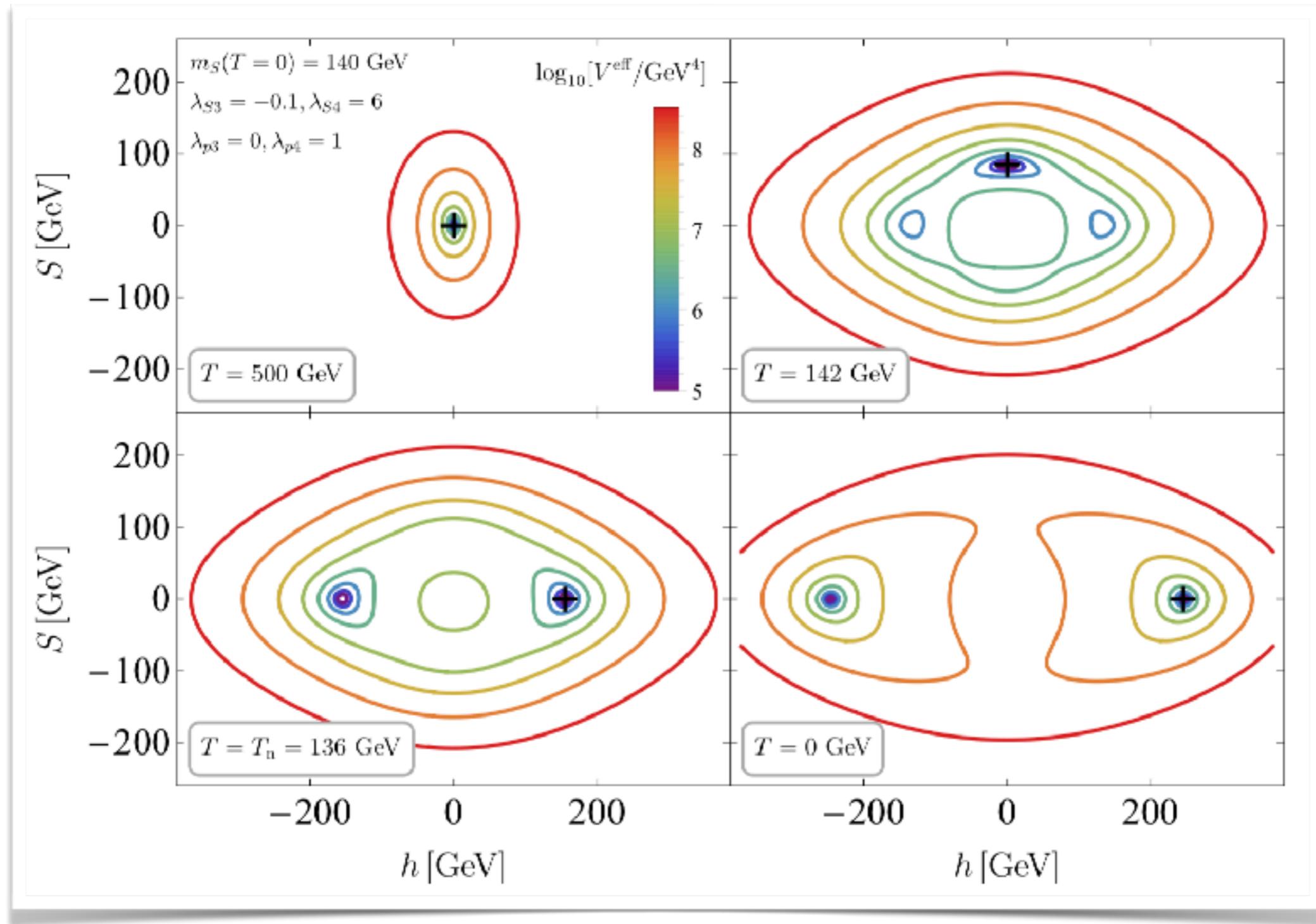
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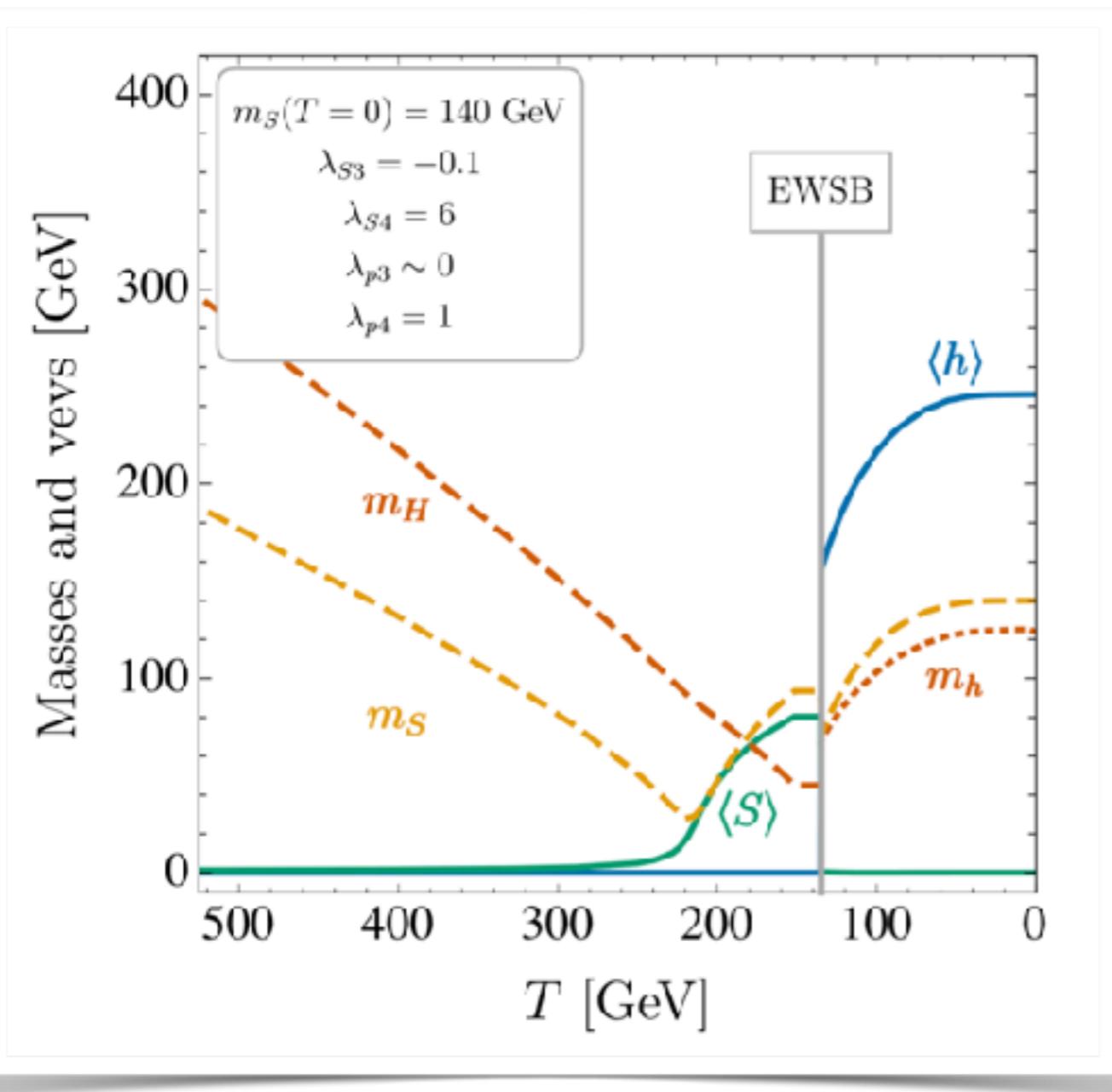
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Vev Flip-Flop in the Scalar Potential

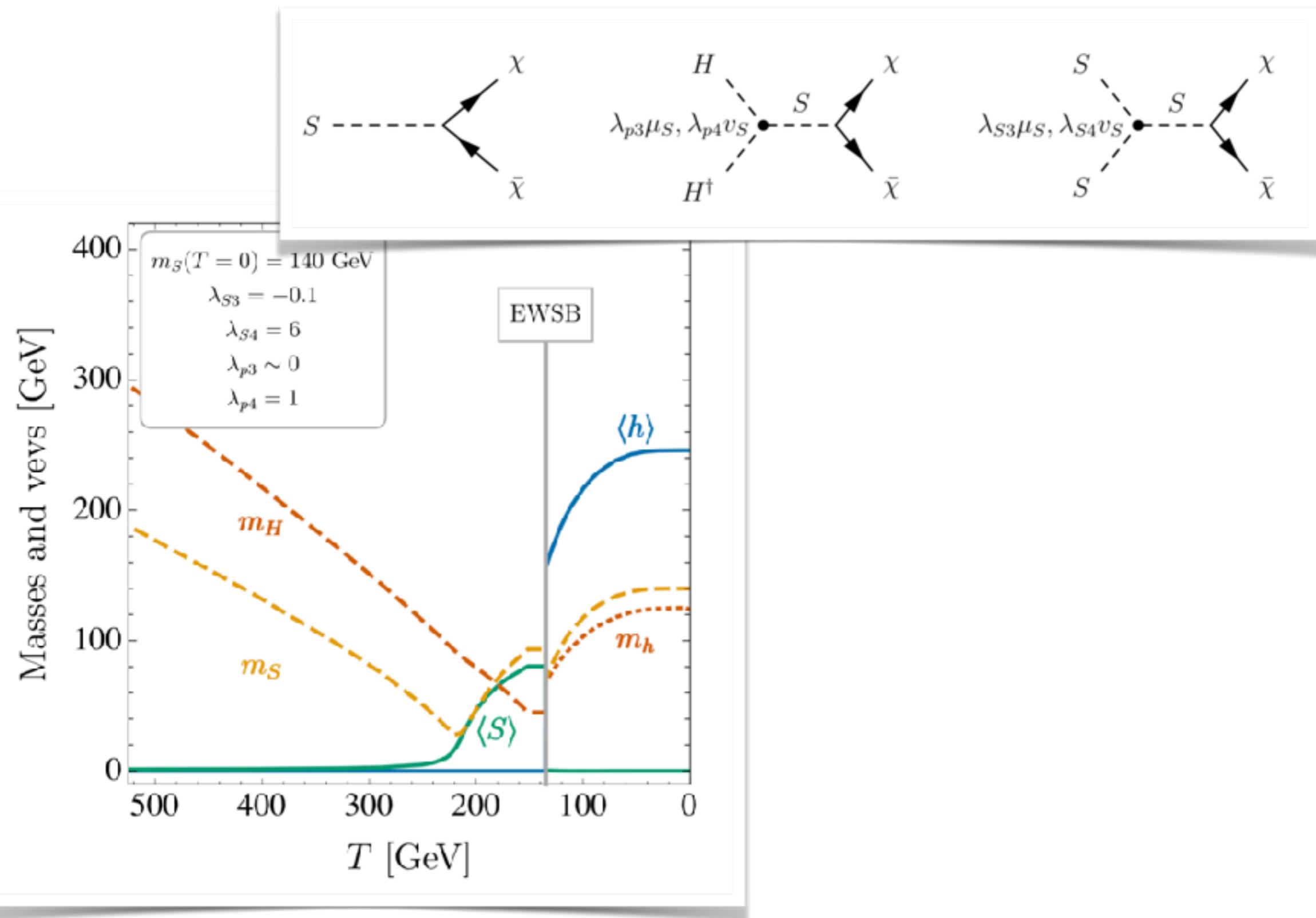


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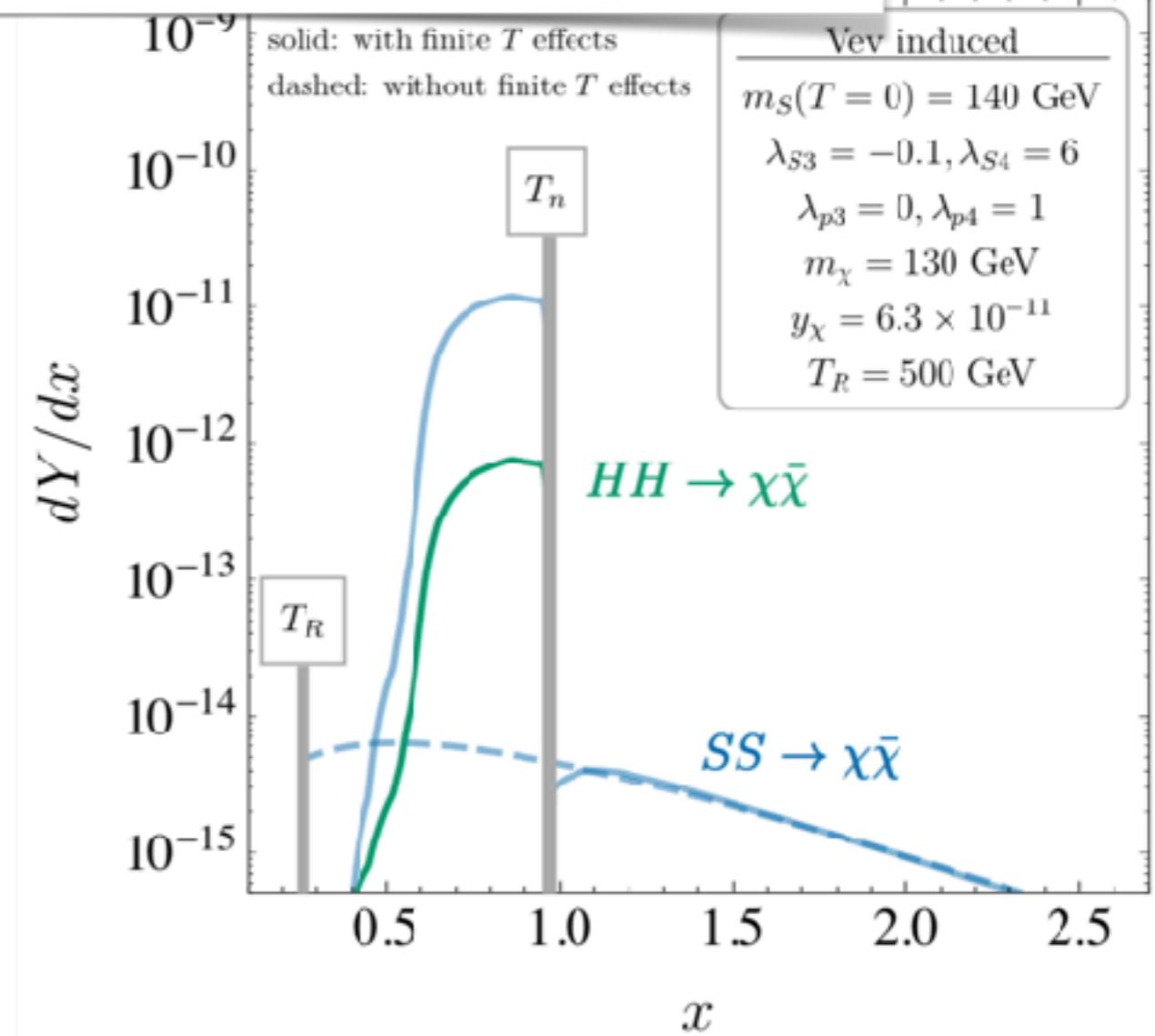
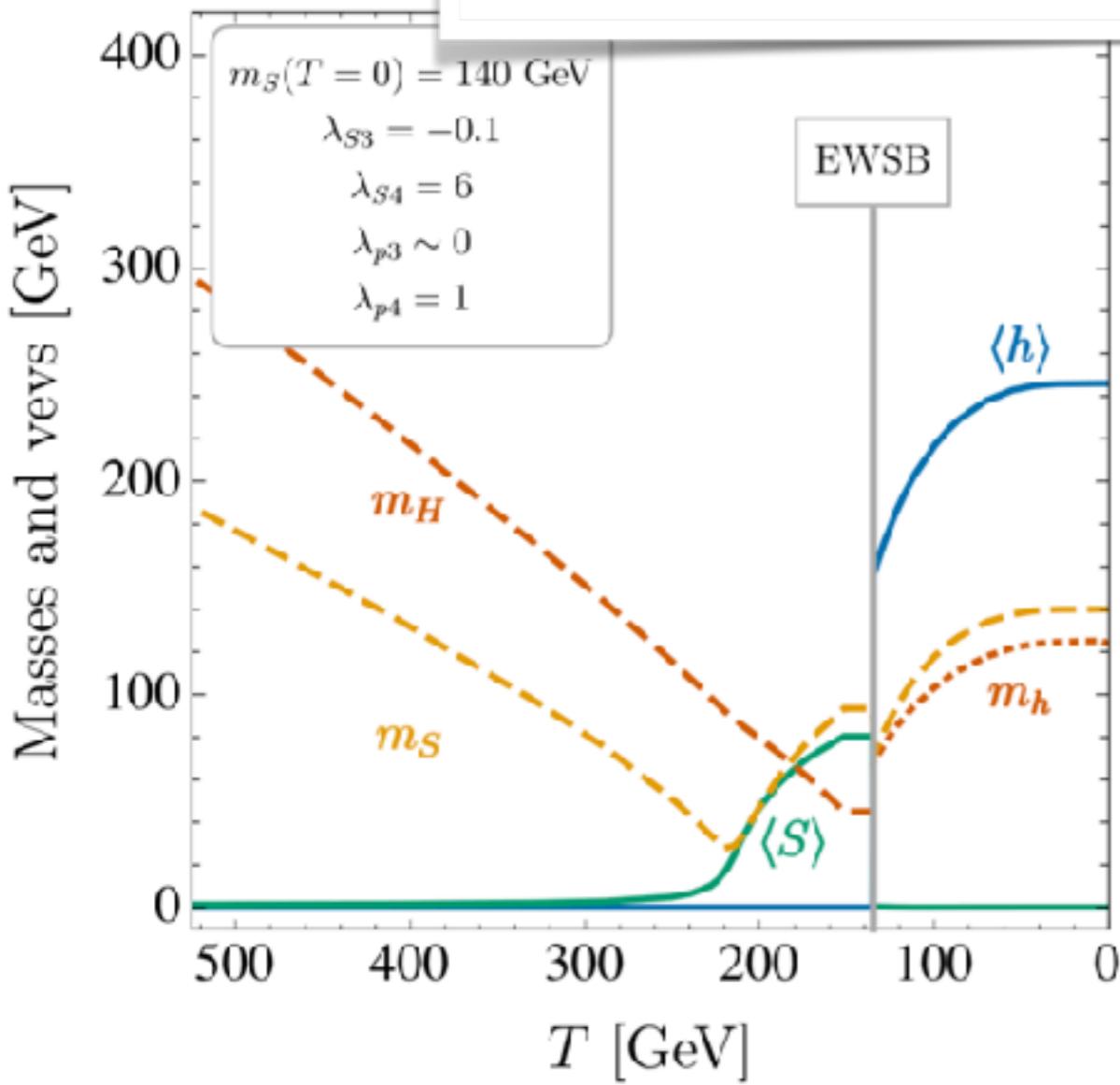
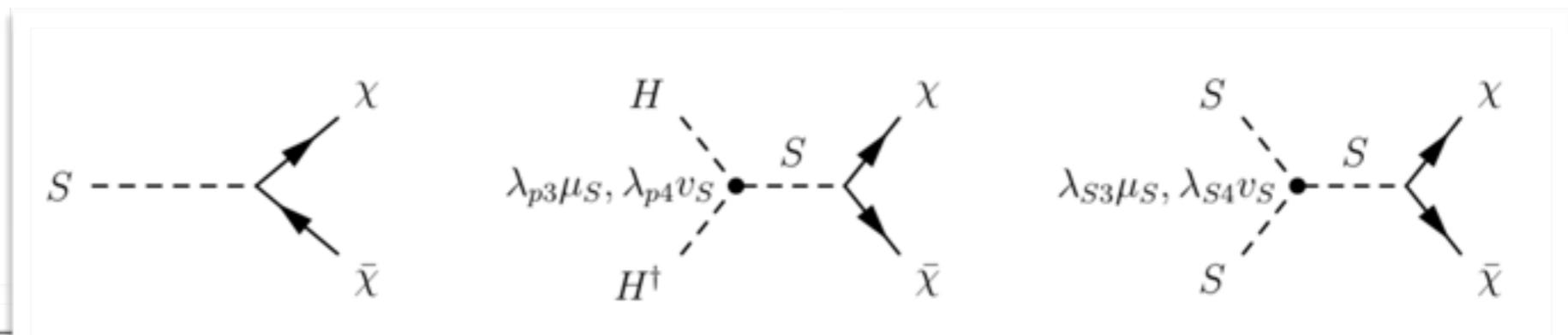
Scalar Masses and Vevs, DM Freeze-In



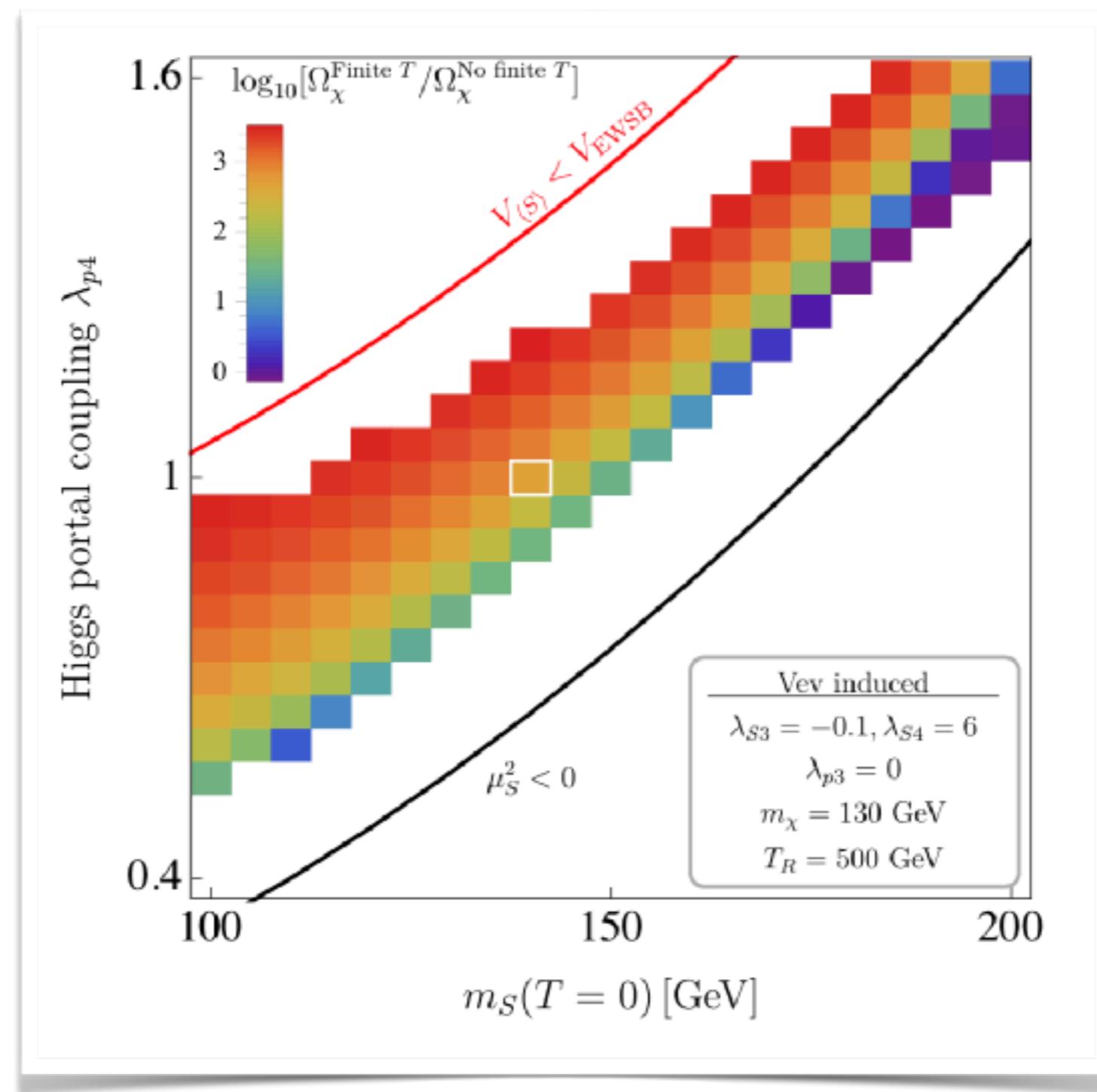
Scalar Masses and Vevs, DM Freeze-In



Scalar Masses and Vevs, DM Freeze-In



Impact of Finite-T Effects: Parameter Scan



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Summary

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Thermal Effects in the Early Universe

- can (temporarily) affect DM stability via phase transitions
- can affect kinematics of freeze-in
- can open/close production channels in phase transitions
- DM abundance may crucially depend on thermal effects

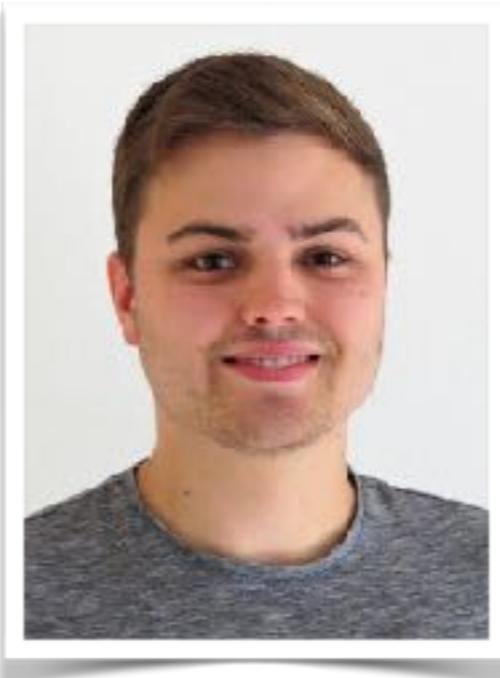
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Mike Baker



Moritz Breitbach



Lukas Mittnacht

Thank you!